

Eco-evolutionary dynamics: multilevel evolution

Course Computational Biology 2025; Paulien Hogeweg; Theoretical
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Last time

- Hypercycles were proposed as potential "ecosystem based" solution for *error catastrophe*
- Studied as ecological system (no ongoing mutations)
- ODE model: vulnerable to parasites *Parasite catastrophe*
- CA model: selforganization in spiral waves ($N > 5$); Dynamics of spiral waves drives parasites to extinction
- All properties of ODE and CA models modeling the same interactions are opposite due to **multilevel selection**
- HOWEVER no solution for error threshold: spiral vulnerable for ongoing mutations
- spiral new level of selections but not new level of replicators.

TODAY: *can we do better??*

Multilevel evolution

- CA Universe: (cf. Crutchfield, Wolfram)
Micro – > Macro (.... – > – > etc)
STATIC (simple) 'rockbottom' **?one more soul?**
- BUT: In evolving systems also Macro – > Micro:

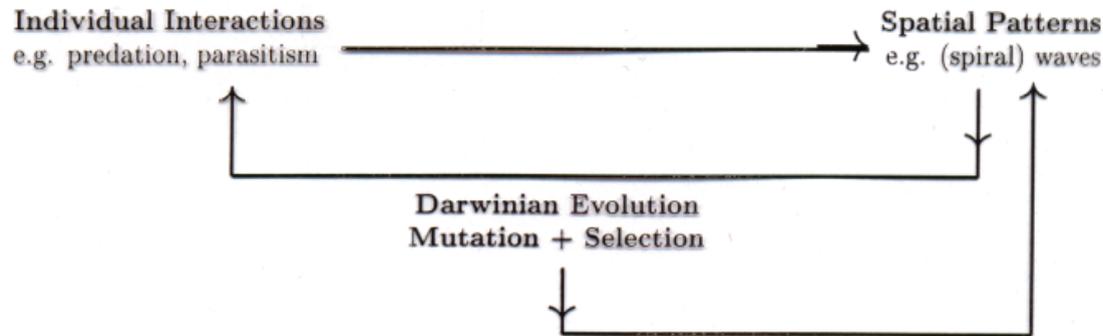


Figure 1: Relation between local interactions and spatial pattern formation in eco evolutionary models

lowest level

does not make sense except in the light of

higher level processes

Themes

*Evolutionary dynamics:
ongoing mutations, selection but no predefined fitness
criterion*

Multiple - Multilevel selection models

Emergent higher level Darwinian entities vs
Imposed higher level (Darwinian) entities

Analysis of multilevel evolution models (ODE as tool)

Degrees of freedom of evolutionary systems

Role of parasites

*“Nothing in biology makes sense except in the light of
Evolution, selforganization ... and parasites*

Ecosystem based information conservation examining the parasite catastrophe beyond hypercycle model

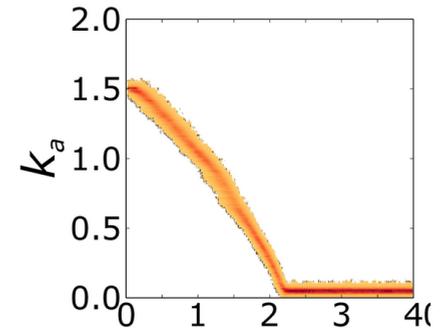
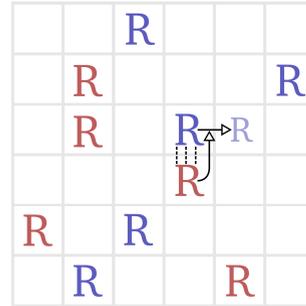
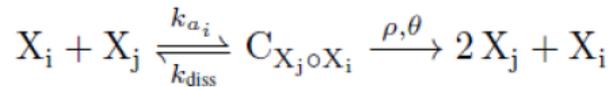
Hypercycle model has in fact
Contrived initial conditions
(multiple species/ specific catalytic interactions)

Here we simplify

Non-cyclic interaction structure.

Ongoing mutations instead of invasion dynamics

Evolution of Replicases (and parasites)



replicases only: Evolve k_{ai}
 well mixed: extinction in space: minimization of k_{ai}

Role of parasites

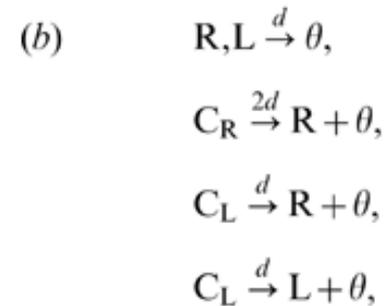
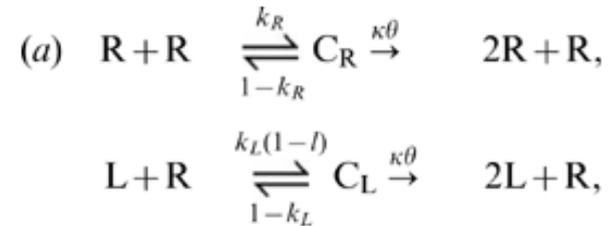
evolve parasites in fixed replicase population

evolve replicases with different fixed parasitic population

co-evolve replicases and parasites

Evolving parasite strength emerging higher level of “Darwinian entities”

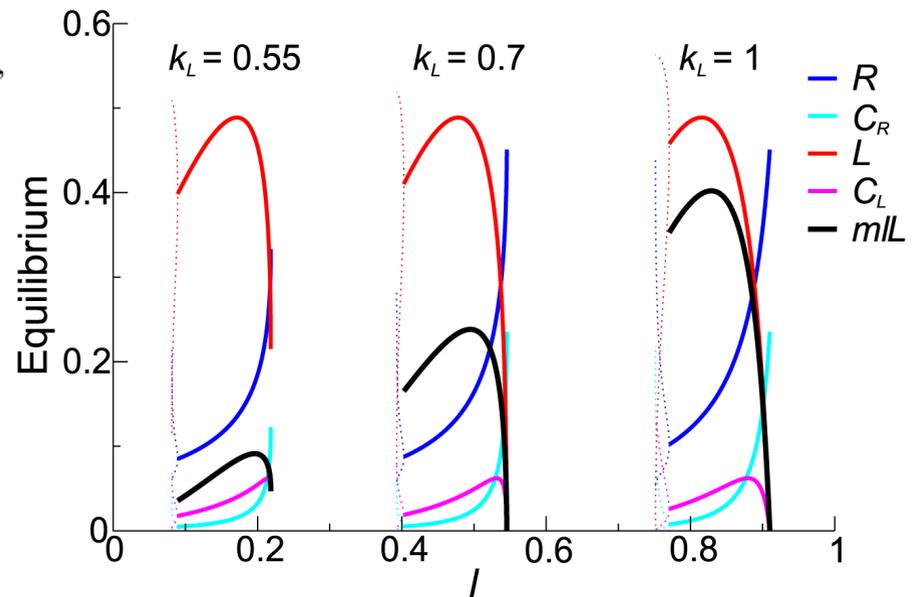
Minimal replicase system (catalysed replication)
with parasitic L's
replicated when unfolded
'functional' when folded



$$\begin{aligned} \dot{R} &= -2k_R R^2 + [2(1-k_R) + 3\kappa\theta + 2d]C_R - k_L RL \\ &\quad + [(1-k_L) + \kappa\theta + d]C_L - dR, \\ \dot{L} &= -k_L(1-l)RL + [(1-k_L) + 2\kappa\theta + d]C_L - dL, \quad (2) \\ \dot{C}_R &= k_R R^2 - [(1-k_R) + \kappa\theta]C_R - 2dC_R, \\ \dot{C}_L &= k_L(1-l)RL - [(1-k_L) + \kappa\theta]C_L - 2dC_L, \end{aligned}$$

Classical problem ODE model of RP system evolutionary extinction (increase of k_L and decrease of l)

$$\begin{aligned} \dot{R} &= -2k_R R^2 + [2(1-k_R) + 3\kappa\theta + 2d]C_R - k_L RL \\ &\quad + [(1-k_L) + \kappa\theta + d]C_L - dR, \\ \dot{L} &= -k_L(1-l)RL + [(1-k_L) + 2\kappa\theta + d]C_L - dL, \quad (2) \\ \dot{C}_R &= k_R R^2 - [(1-k_R) + \kappa\theta]C_R - 2dC_R, \\ \dot{C}_L &= k_L(1-l)RL - [(1-k_L) + \kappa\theta]C_L - 2dC_L, \end{aligned}$$



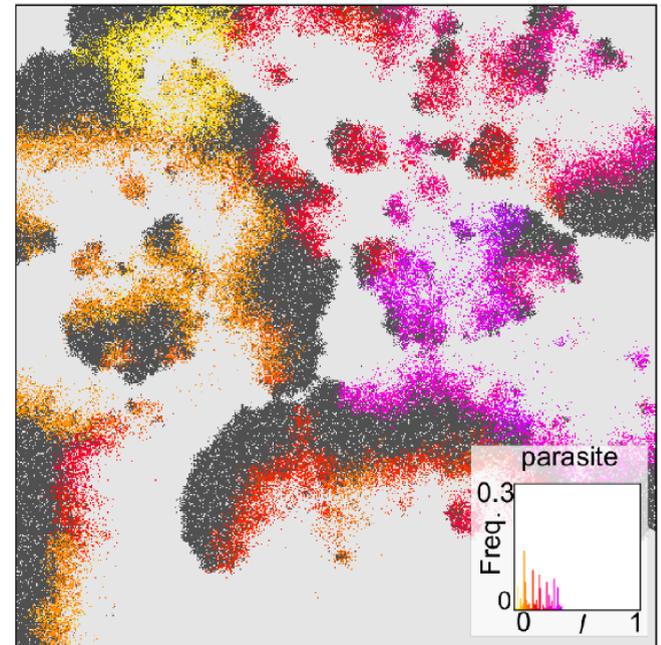
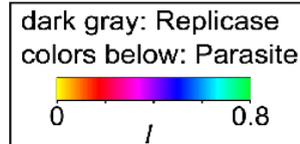
intrinsic advantage of parasite (L)

CA model of RP system evolutionary stable (long transient)

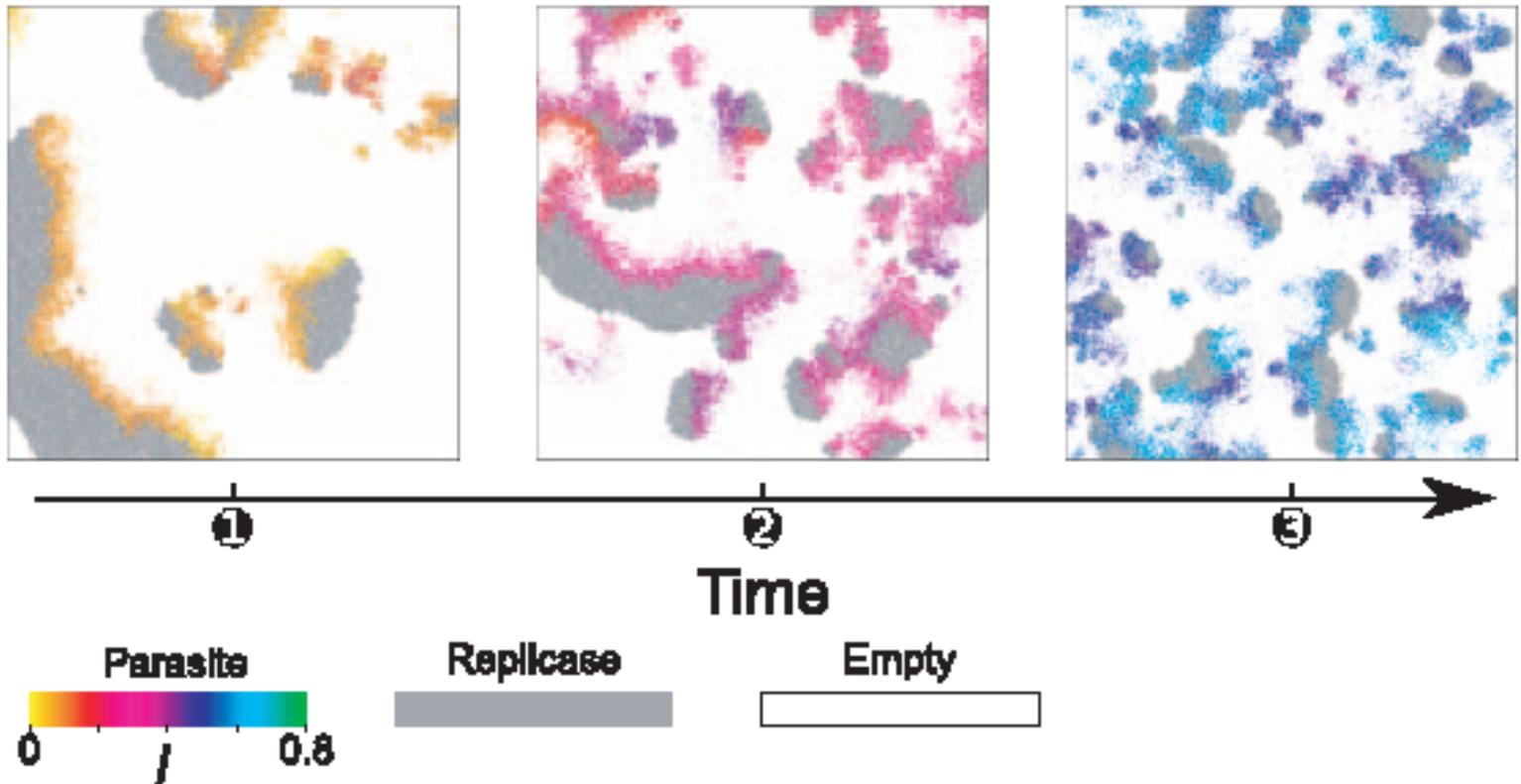
Asynchronous CA choose random patch and random NB
perform reaction or diffusion

reaction: (complex formation (coupling 2 gp),
replication and decay))

with prob. according to
individual (evolving) parameters
of *parasites*: K_l and l

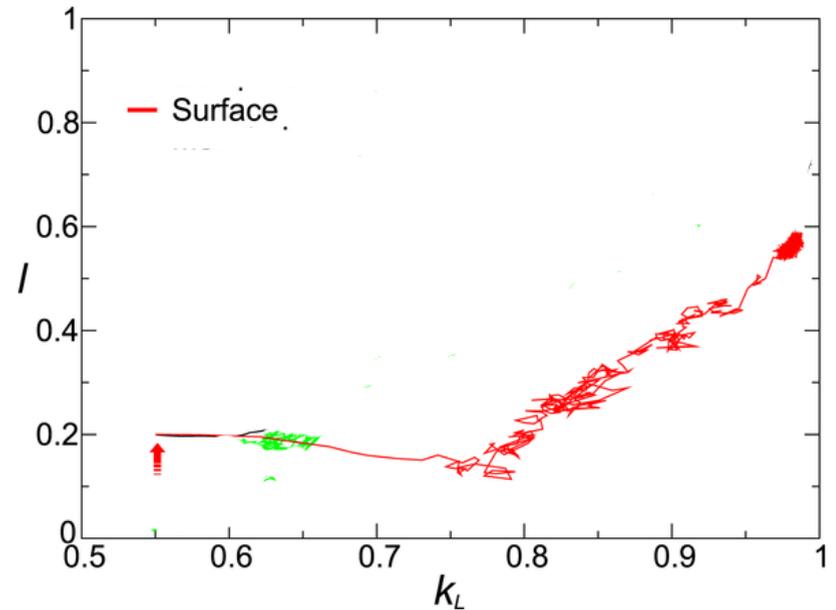
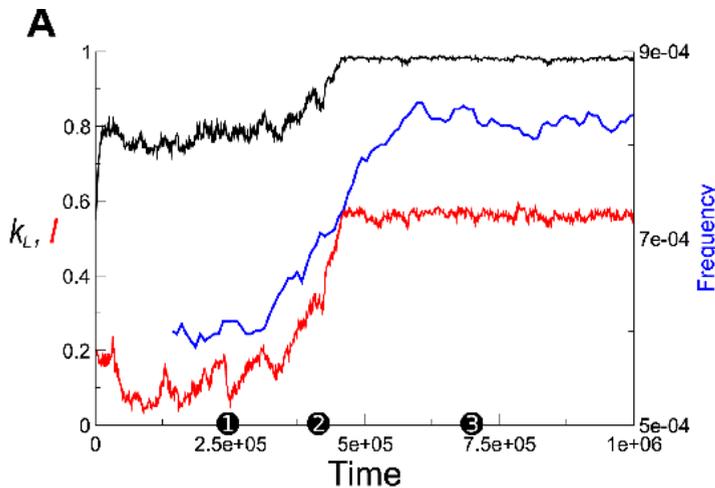


long term evolution: towards smaller waves



Long term evolution (parameters) emergent 'trade-off' k_L and I Maximizing I : potential 'new' function

Average in population

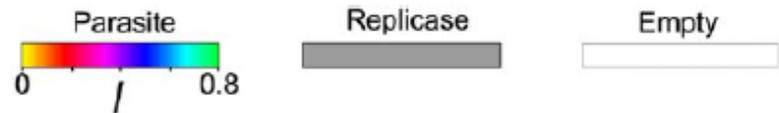
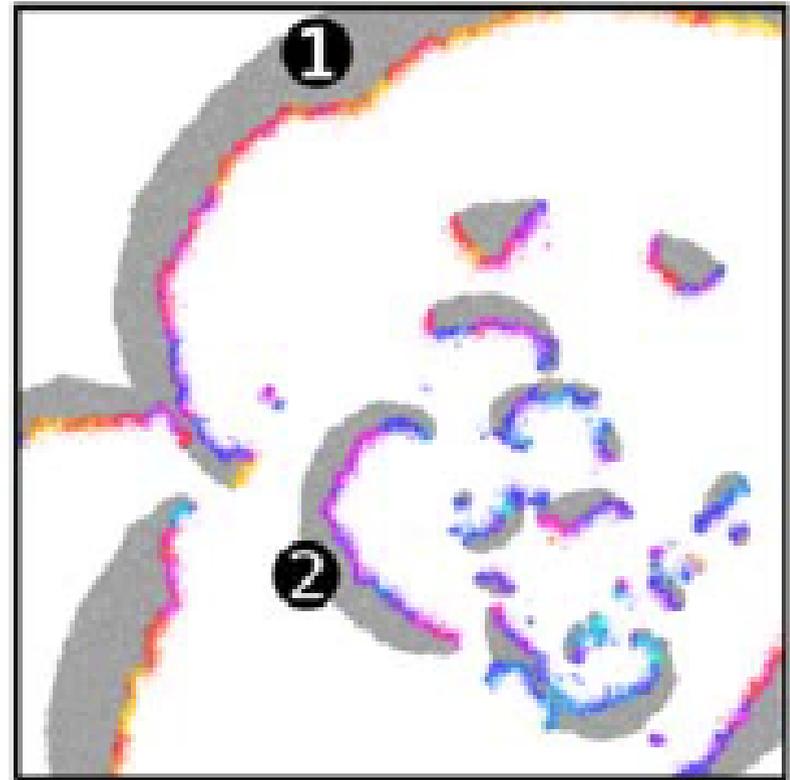


WHY?

evolution of higher level entities

The waves of replicase and parasites are higher level “Darwinian” entities

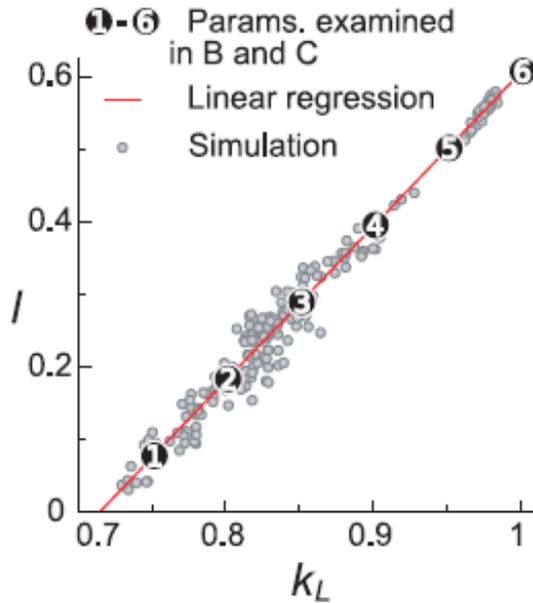
Birth
Maturation
Death
Mutation
Selection
Competing



$$K_L = 1$$

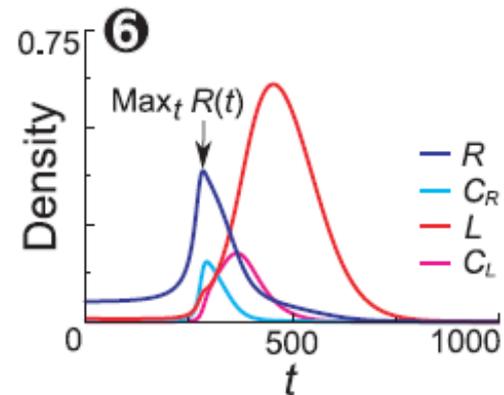
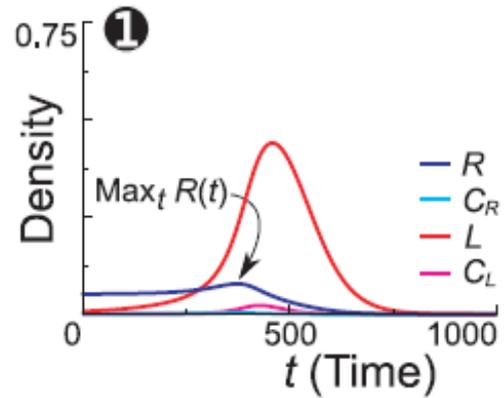
Larger K_L and I increase birthrate of waves analysis of transient in ODE (for evolved parameters)

A



B

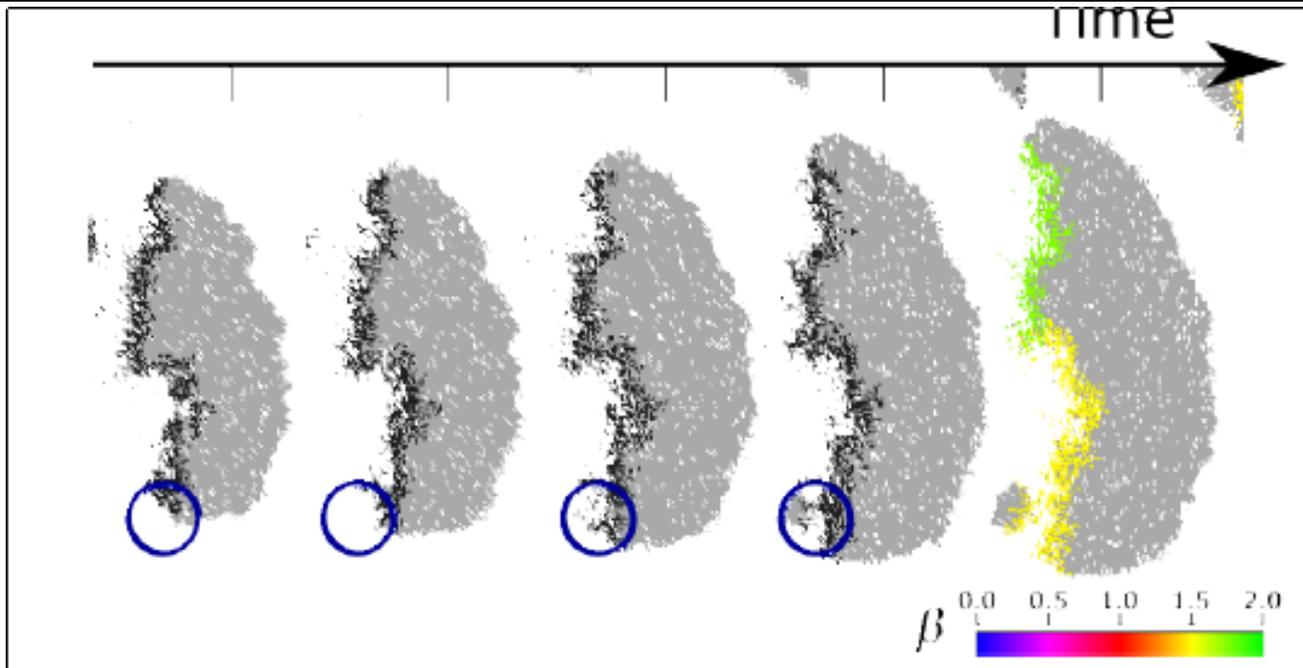
$R(0)=0.055, L(0)=0.0075$
(②-⑤ not shown)



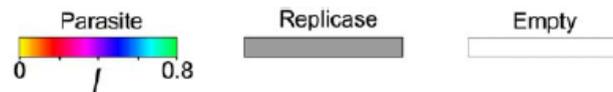
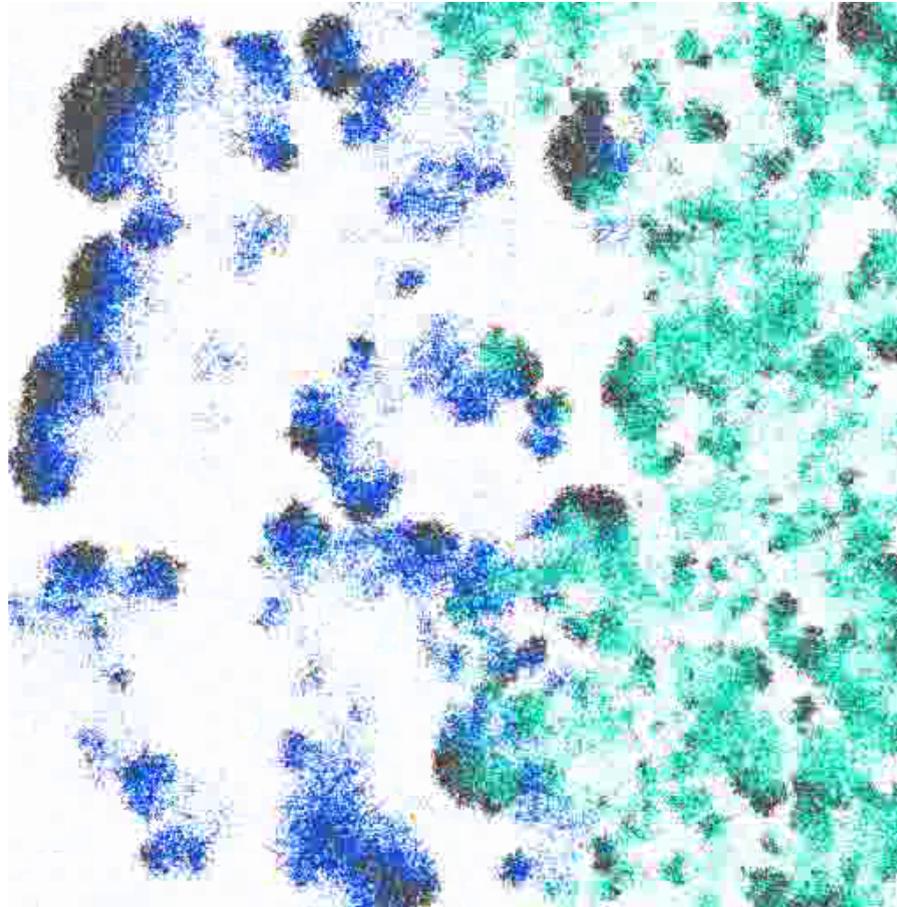
C

0.5

Example of birth of new waves,
happening at relatively weak parasites



evolutionary attractor at “edge of chaos” (“border of order”)



2 levels of Darwinian selection

Wave level evolution

- Waves: long lived -
(death not by parasites but by collision)
- Maximize Birthrate + growth rate of newborns
- Birthrate higher for high I ('escape')
- However higher birthrate – > more (smaller) waves
- – > increase collision! (= deathrate of waves))

Individual level evolution

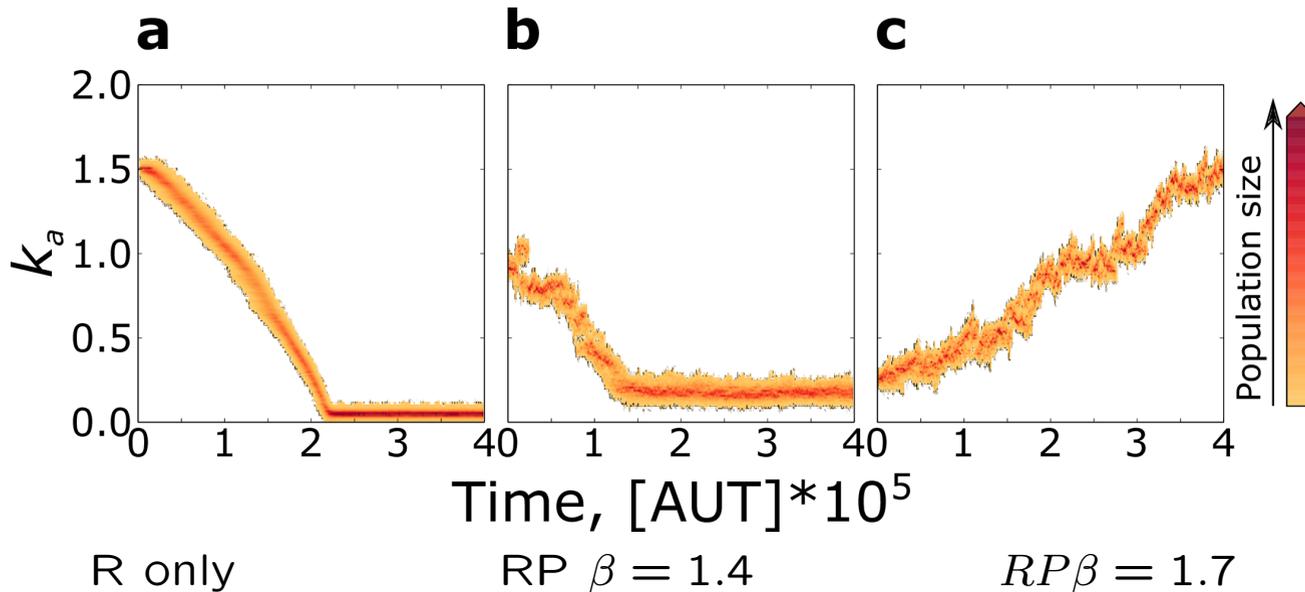
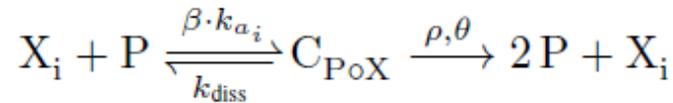
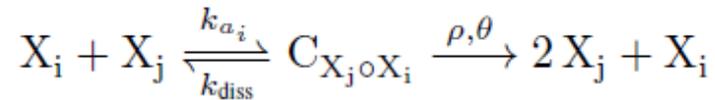
- Within waves: parasites evolve towards 'nastiness' (low I)
- However viability maintained -- >
“prudent” parasites
- because of higher level selection; which also
- 'frees' parasites to do other things (be folded)

*through parasites
evolution of novel functionality*

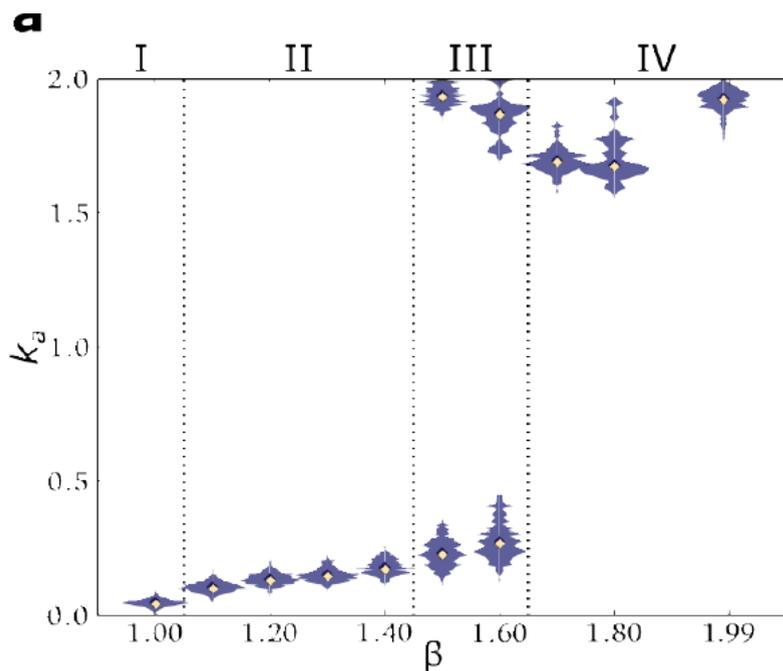
Evolution of replicases in RP system

Strong parasites lead to strong replicases

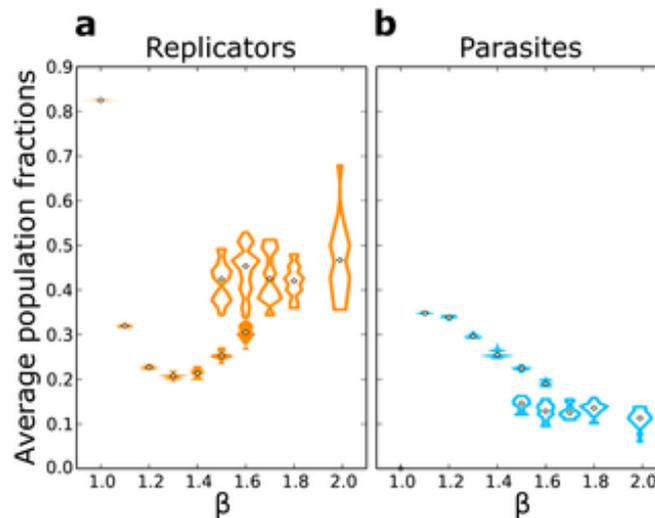
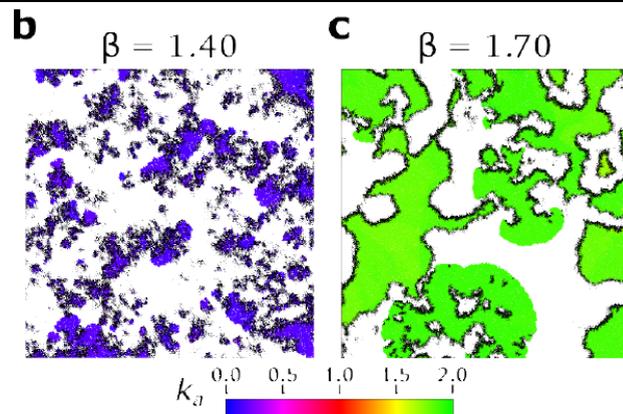
The model



Phase transition and bistability maximizing birth rate of waves OR maximizing invasion rate of empty space



stronger parasites – $>$
more replicases and less parasites



Maximizing invasion of empty space vs maximization of birthrate of waves

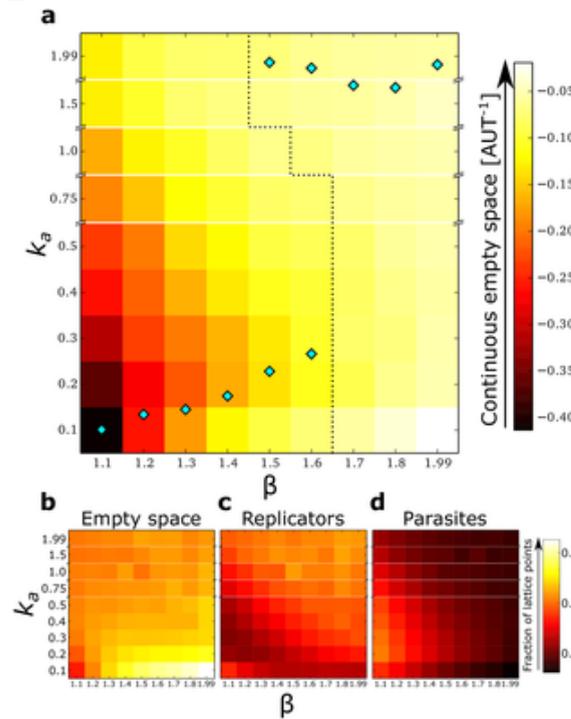
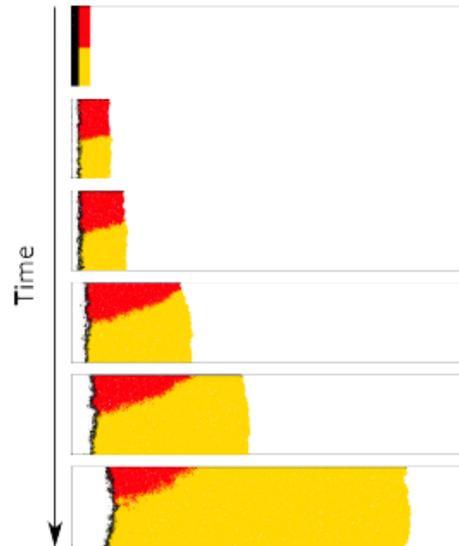
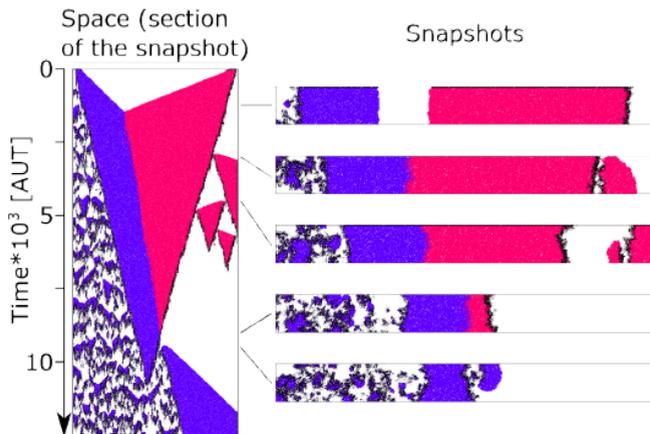
LOW $\beta = 1.3$

blue: $k_a = .2$; red $k_a = .8$

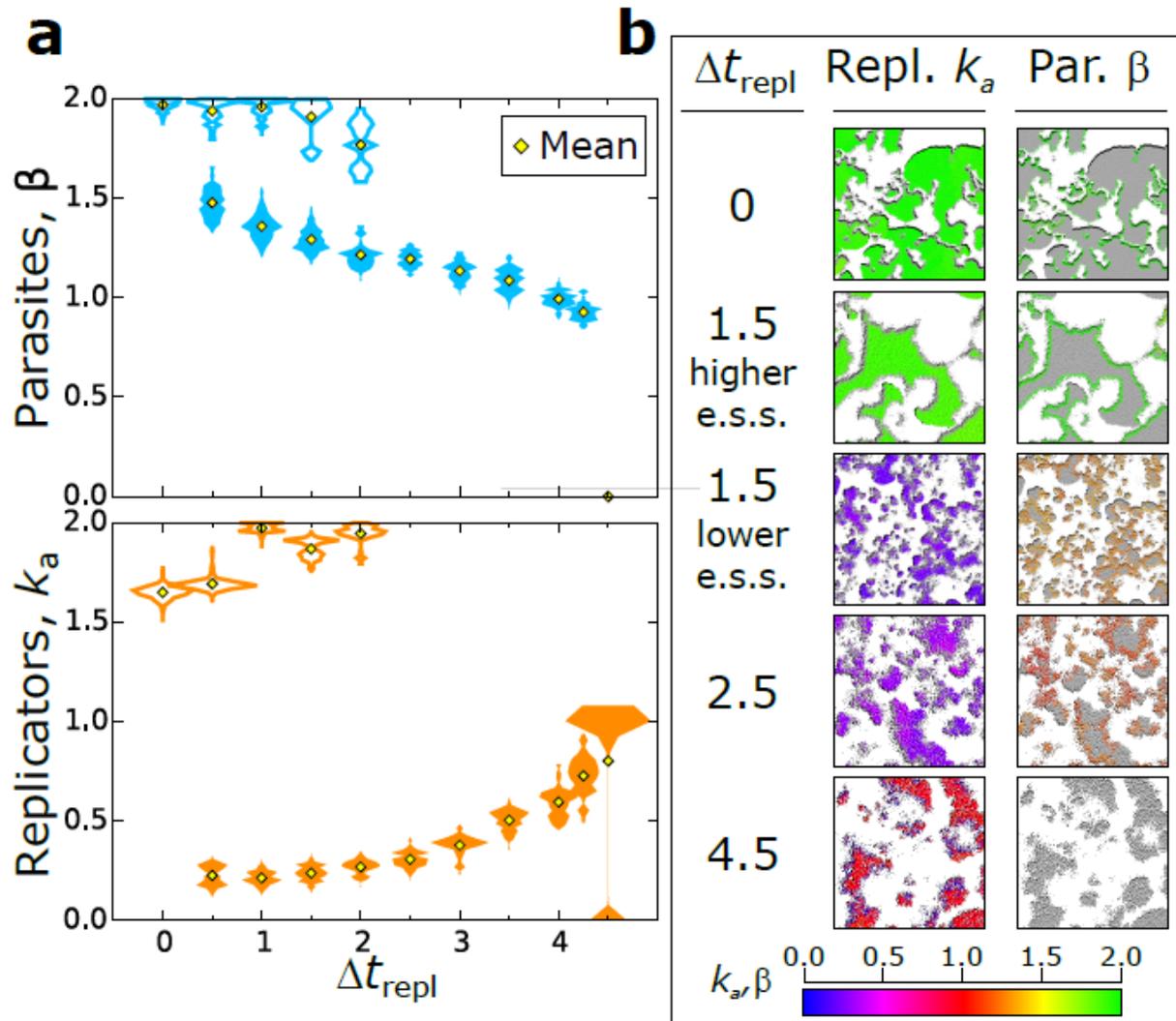
HIGH $\beta = 1.8$

red $k_a = 1$ yellow $k_a = 1.2$

empty space



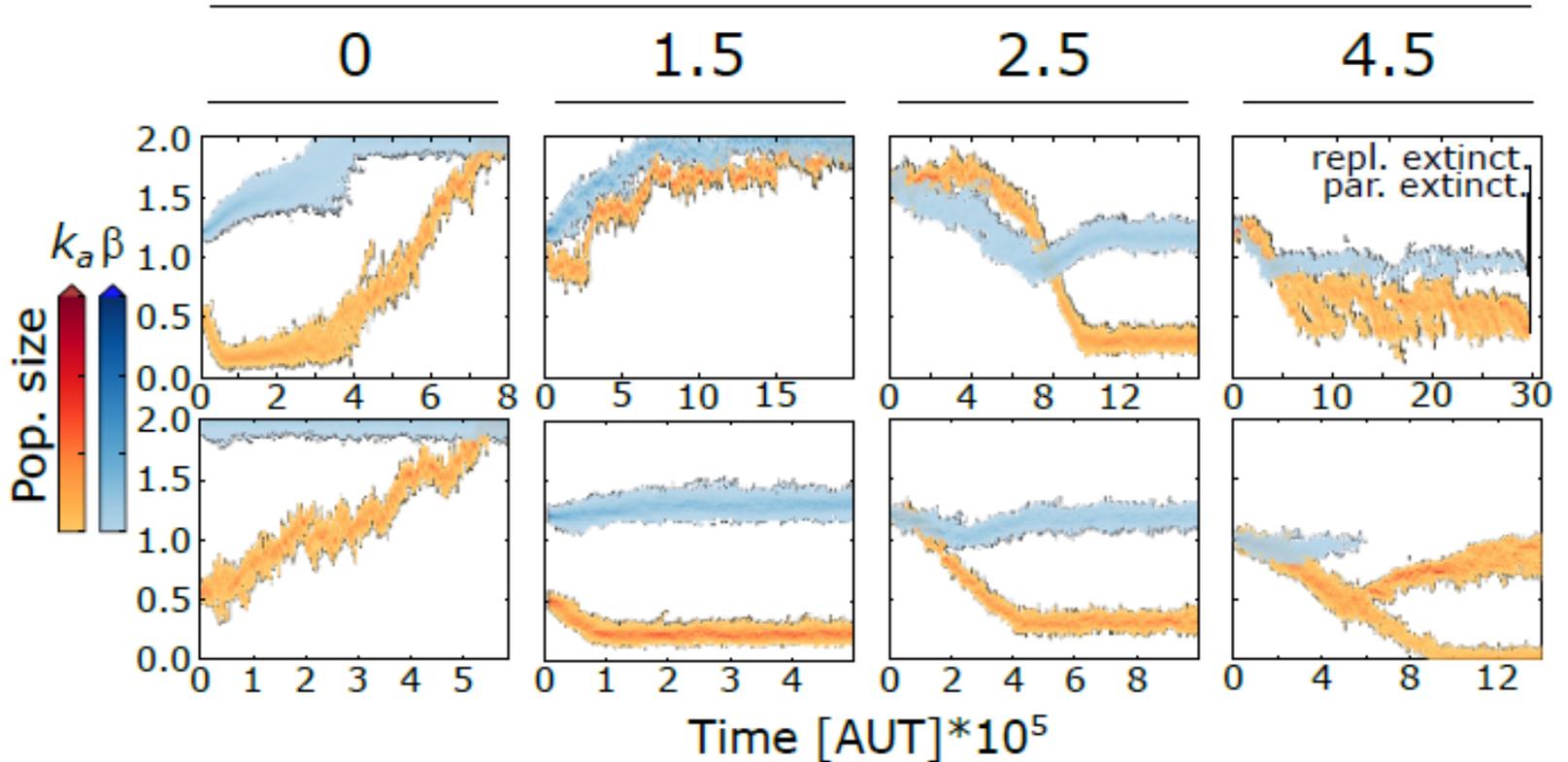
Coevolution of replication (k_i) and parasite strength β



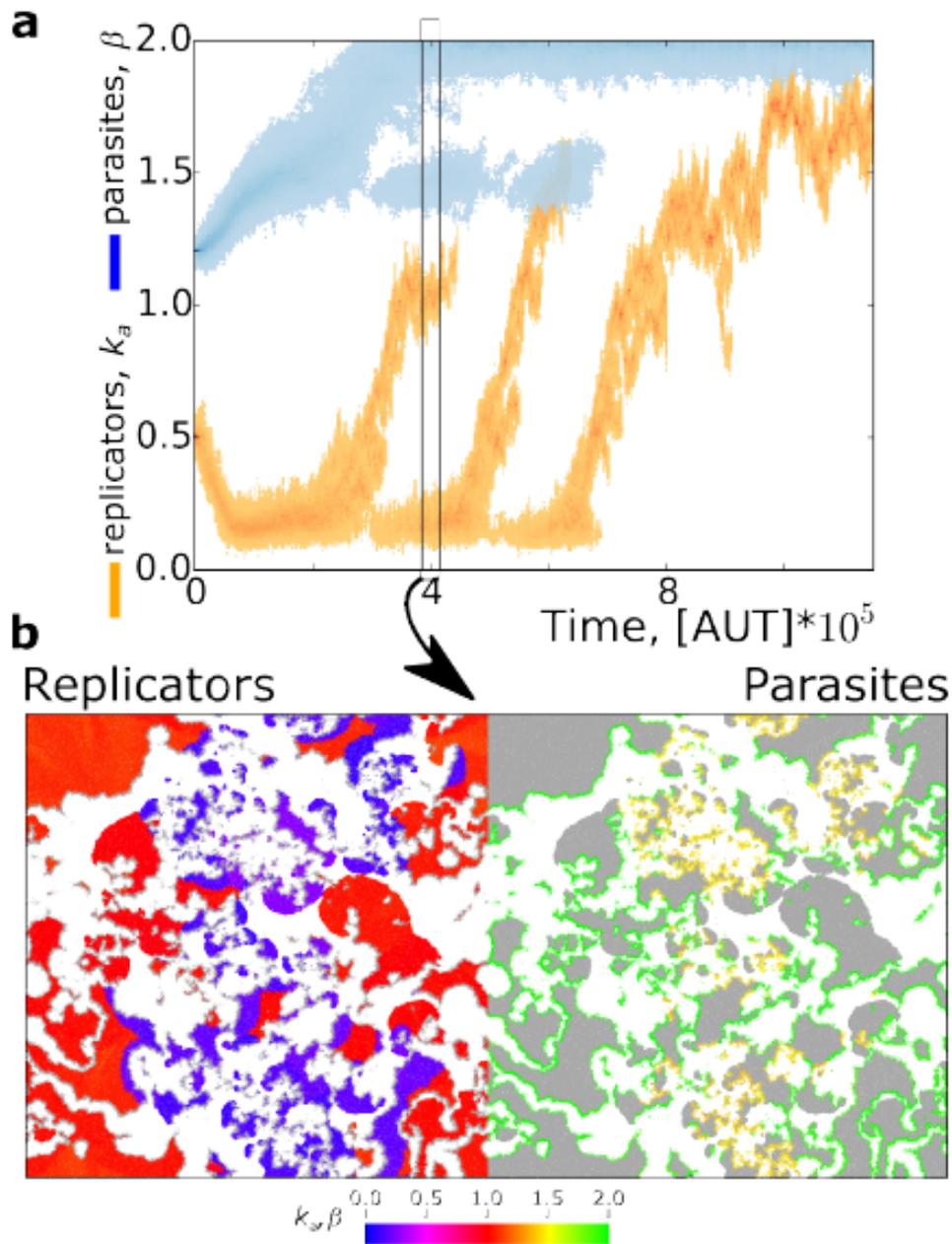
varying duration in complex

coevolution of replication (k_i) and parasite strength β
for different time in complex : timeplots

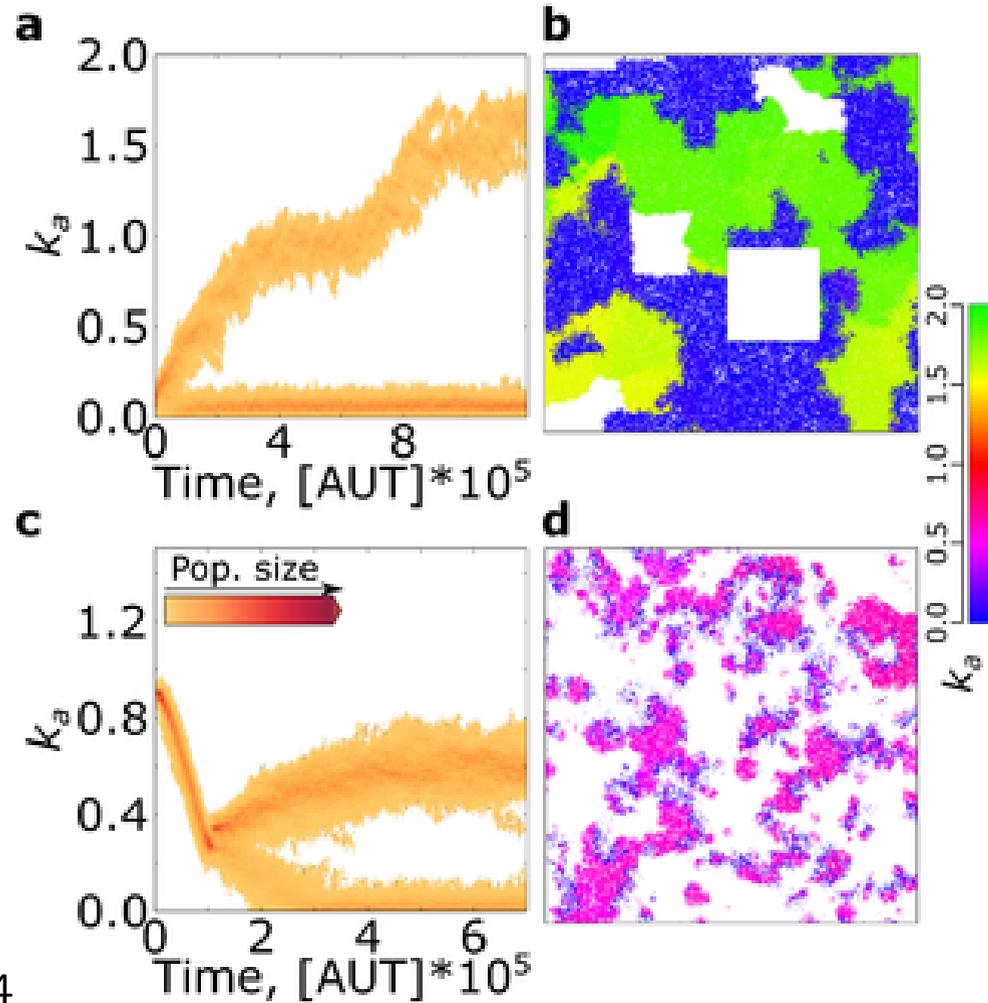
Δt_{repl}



$\Delta T_{repl} = 0$
"Ghost" attractors
(bistability)



Speciation:
From replicases only to replicases and parasites
Disruptions or cost (duration) of replication



$$\Delta T_{repl} = 4$$

conclusion

*Because of wave-level selection
Parasites enhance replication potential*

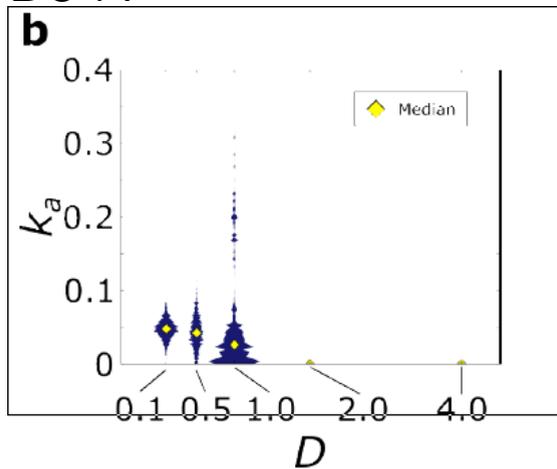
Bistability:

*maximizing birth rate of waves
minimizing 'altruism'*

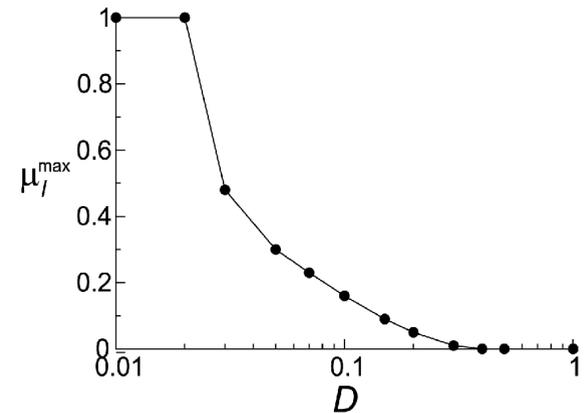
vs
vs

*maximizing wave stability
maximizing invasion rate*

BUT:



limited diffusion (replicase model)



errorthreshold (parasite model)

conclusion

Emerging higher level Darwinian Entities (waves)

in minimal eco-evolutionary replicator RP model:

waves emerge because of parasites

waves as evolving entities (birth, death, mutation, selection)

emergent trade-off

bistability; parasitism induces more catalysis

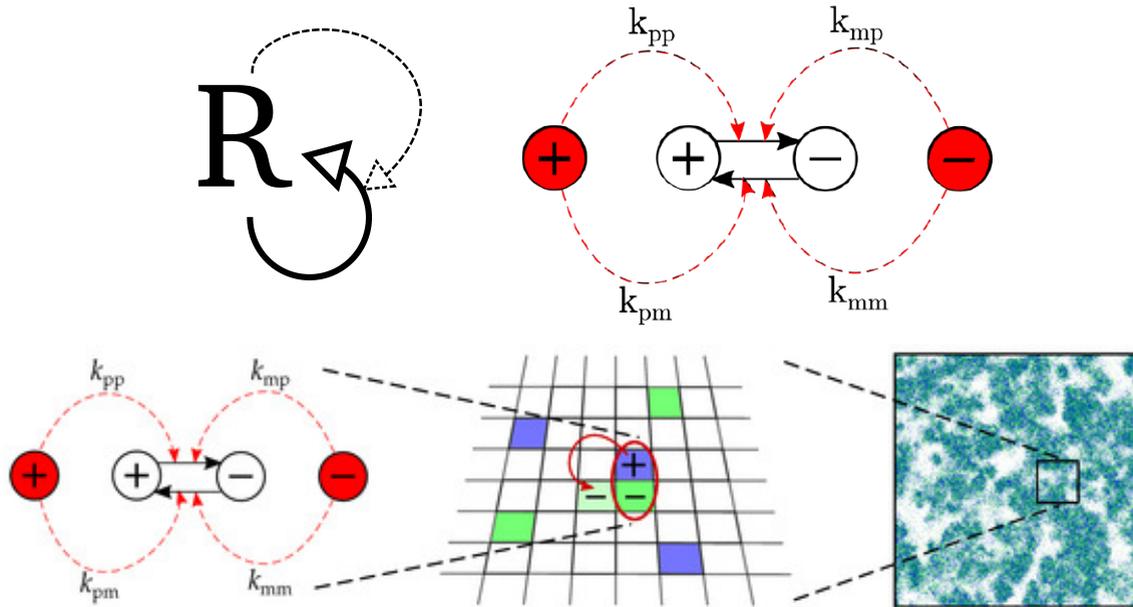
, potential of novel function

parasites emerge in disturbed environments

and when giving catalysis is costly enough

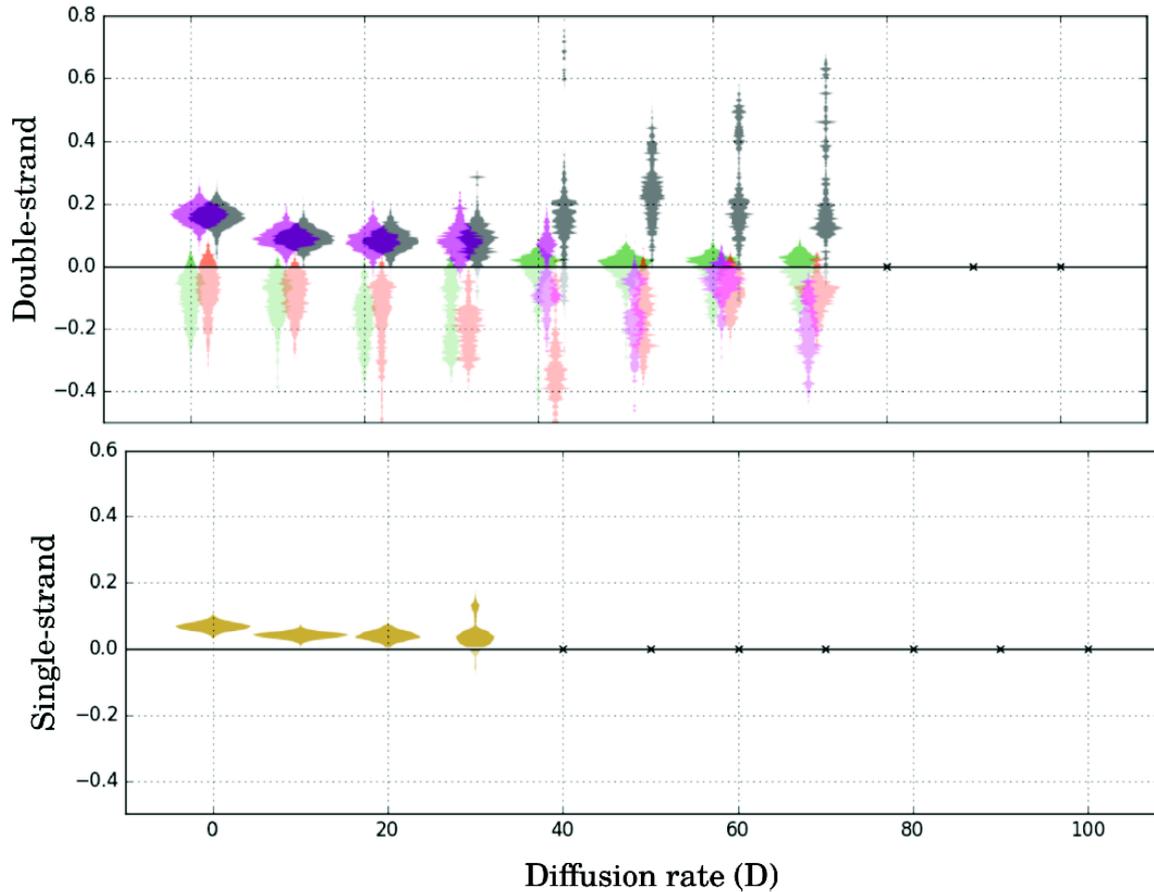
exploring evolutionary properties/advantages of more RNA-like replicators in R-only system (i.e. more degrees of freedom)

- Direct replication vs Complementary replication

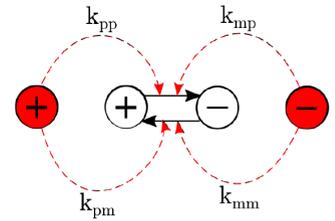


1 vs 4 evolving parameters: K_{xx} vs $K_{pp}K_{pm}K_{mm}K_{mp}$

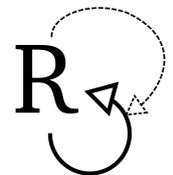
emergent levels of selection
 direct vs complementary replication
 symmetry breaking robustness to diffusion



- k_{pp}
- k_{mm}
- k_{pm}
- k_{mp}



- k_{xx}



symmetry breaking and speciation

von den Dunk, Colizzi Hogeweg 2017

initial decrease
of catalysis

Only if small
enough
emergent
higher level
selection
leads to

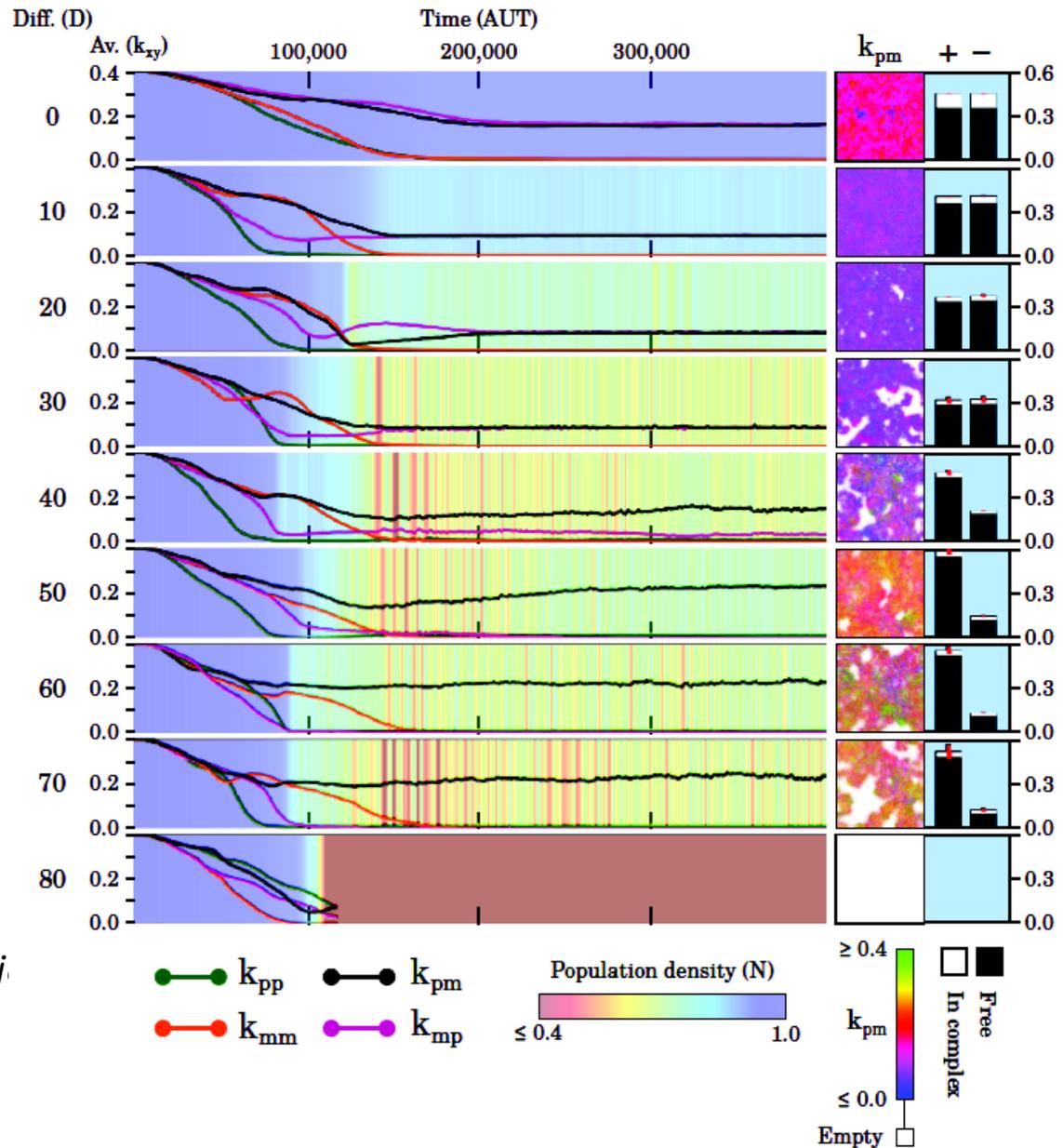
3 types of
symm breaking:

reciprocal
($K_{pm} - K_{mp}$)

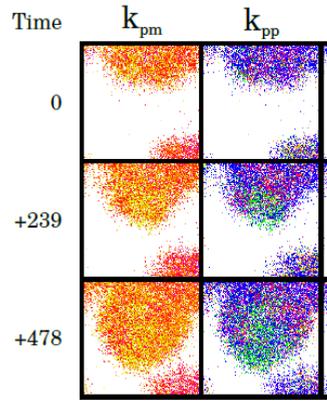
target
($K_{pm} - K_{mm}$)

one-cat
($K_{pm} +$
 $\ll K_{pp}$)

LOSS of functi

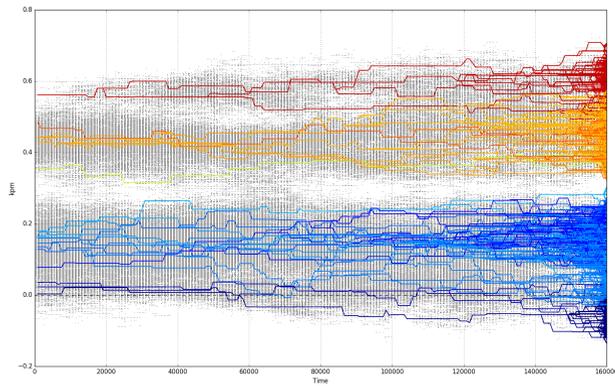


Evolutionary dynamics at high diffusion (D70)

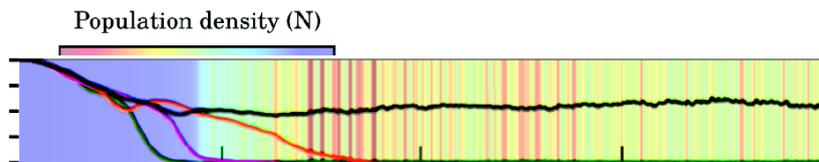


selection at wave front

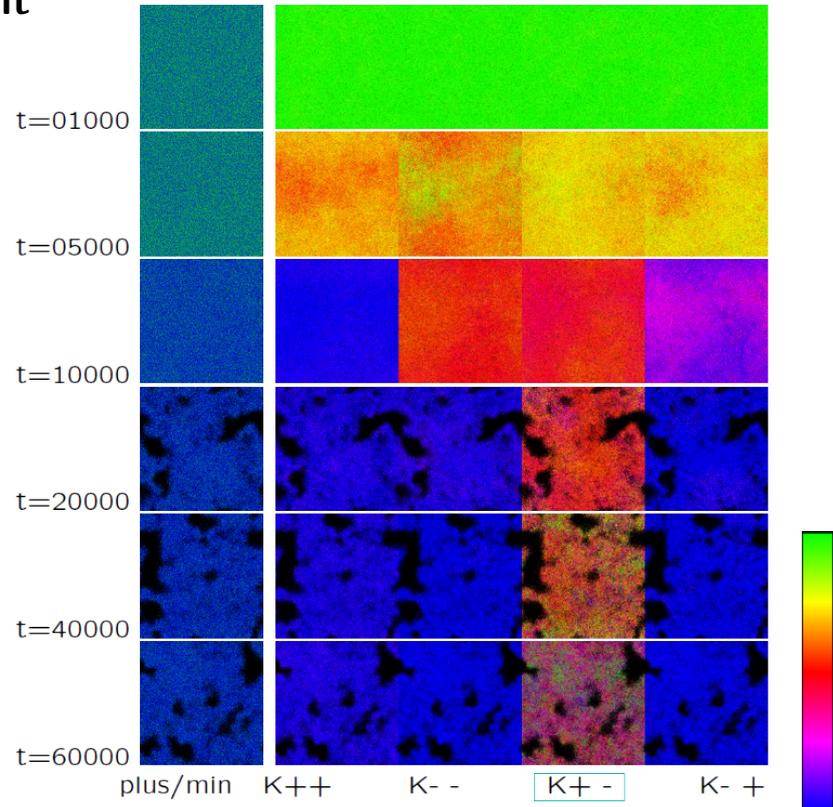
ancestor trace



evolution through time



spatial self-organization



Conclusion

Symmetry breaking and division of labor to resolve conflict between high catalysis and being template

Exploit “near death” for evolving new replication strategies

creation of wave-fronts and positive selection for more catalysis
(wave-level+individual level)

evolved parasite lineage essential for survival:

enabling wave-formation - multiple 'niches'/selections pressure

Exploit complementary replication for “division of labor”

Always symmetry breaking, different kinds

At high diffusion

One catalytic strand (+), strongly favors complementary strand (-)

Many +, few - strands (Genome-like)

Therefore less selection to minimize catalysis

optimizes both availability as template and amount of catalysis
(wave front/wave back)

maximizes evolvability to adapt to wavefront (increase K_{++})

Evolution of multiple lineages (speciation)

mutual dependence (feedback) higher level/lower level evolution

conclusions

Less well defined, distinct “level of selection”

Conflict resolution between levels

Multiple niches

More evolutionary degrees of freedom: BETTER results:

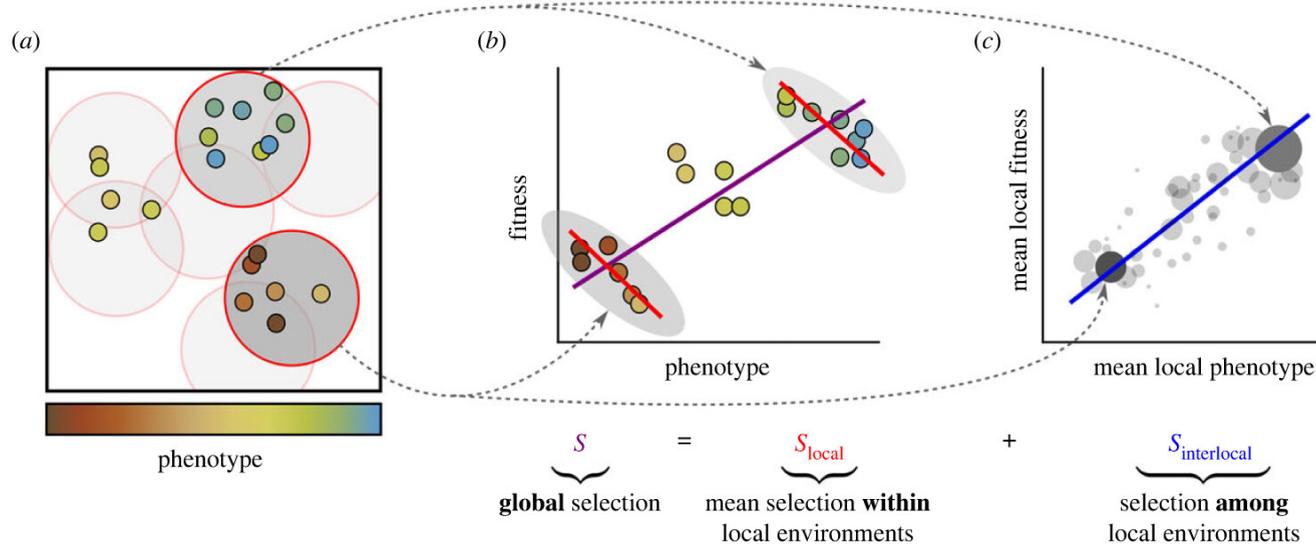
*here: higher diffusion
higher mutation rates (not shown)*

Quantifying selection at different scales

Multiscale selection in spatially structured populations Hilje M. Doekes and Rutger Hermsen 2024

define selection of a trait as the covariance between the trait value and the number of offspring after a period δt . (Pierce equation)

measure selection at in areas of different size different locations.



$$S = \mathbf{mean}(\text{LSD}) + \mathbf{Cov}(\text{local mean}(\phi), \text{local mean}(w))$$

$$\equiv S_{\text{local}}(r) + S_{\text{interlocal}}(r),$$

Example: SI (susceptible-infectious) model in space

