Large scale Event based model & Gene regulatory network models

Course Computational Biology 2025; Paulien Hogeweg; Theoretical Biology and Bioinformatics Grp Utrecht University Last time:

CA as modeling tool

- generalizations of CA ss
- baseline expectations: "pattern default"

CA and ODE/MAP's as dynamical systems

- alternative simplifications
- common features (types of attractors etc.)
- Qualitative and quantitave different behaviors:
- Example birth death processes.
- Population based vs individual based
- Mean field approximation/assumption

Event based systems: Gillespie algorithm

- (average) cellcycle time and/vs growth rate

TODAY

Event based systems cont.:

example: large scale "whole cell" modeling of translation

modeling in terms of subsystems (cont)

Network models

Boolean networks as model for gene regulatory networks:

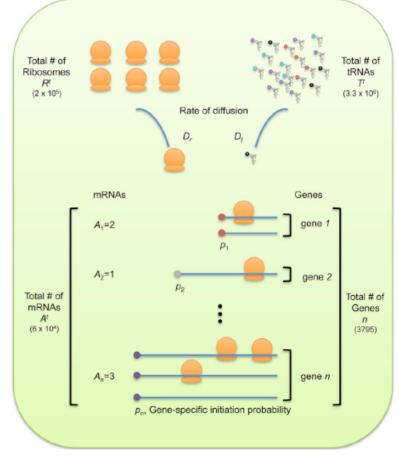
- multiple attractors (= celltypes)
- domains of attraction, reachability, alternative transients.
- Understanding/interpreting gene knockouts
- inference of GRN from transcriptomics data
- minimal vs "real" networks
- non-network properties of GRN

Large scale, data driven EVENT based models: continuous time, discrete events Gillespie algorithm

seen as multi-entity - multistate decomposition

Example

Rate-Limiting Steps in Yeast Protein Translation P Shah, Y Ding, M Niemczyk,



DATA

- fasta file of yeast mRNA + number of mol/cell
- yeast tRNA's (41) + number in cell + wobble
- number of ribosomes
- initiation prob of all mRNA types
- size of ribosome/tRNA's yeast cell
- diffusion constant ribosomes, tRNA's
- --> characteristic times

STATES

- number of free ribosomes/tRNA's(of every type)
- Position of each bound ribosomes/tRNA's on each individual mRNA

EVENTS

- Initiation (binding of ribosome at free 5'end of mRNA)
- Elongation (change postion, free bind tRNA)

Yeast data on cell content

Table 1. Summary of Model Parameters				
Parameter	Description	Value or Range of Values	References	
R ^t	number of ribosomes	2 × 10 ⁵	(Warner, 1999; von der Haar, 2008)	
A ^t	number of mRNAs	6 × 10 ⁴	(Zenklusen et al., 2008)	
T ^t	number of tRNAs	3.3 × 10 ⁶	(Waldron and Lacroute, 1975)	
Tn	number of types of tRNAs	41	(Chan and Lowe, 2009)	
T_j^t	number of tRNAs of type j	~12,000–190,000	(Chan and Lowe, 2009)	
A _i	number of mRNAs of type i	1–1,254	(Ingolia et al., 2009)	
p i	gene-specific initiation probability	~3.5 × 10 ⁻⁶ –0.115	(Experimental Procedures)	
n	number of genes	3,795	(Ingolia et al., 2009)	
Dr	diffusion coefficient of ribosomes	$3 \times 10^{-13} \mathrm{m^2/s}$	(Politz et al., 2003)	
Dt	diffusion coefficient of tRNAs	8.42 × 10 ⁻¹¹ m ² /s	(Werner, 2011)	
C _r	size of ribosome footprint in codons	10	(Ingolia et al., 2009)	
s	tRNA competition coefficient	7.78×10^{-4}	(Experimental Procedures)	
V	volume of the cell	$4.2 \times 10^{-17} \text{ m}^3$	(Siwiak and Zielenkiewicz, 2010)	

 $N_t = 1.24 imes 10^7$ and $N_r = 1.56 imes 10^6$,

Algorithm (pseudocode)

while time < t (total simulation time) do

Calculate

Fraction of mRNAs of gene *i* that are *initiable*, f_i - i.e., those mRNAs with first 10 codons unbound.

Number of *elongatable* ribosomes waiting at codon j, $R^b(j)$ - ribosomes with next 10 codons unbound.

Rates of all possible events (see Table S2)

Total initiation rate: $\rho^t = \sum_{i=1}^n \frac{R^f f_i A_i p_i}{\tau_r N_r}$ Total elongation rate: $\epsilon^t = \sum_{j=1}^{61} \frac{R^b(j) T^f_{\phi(j)} w_j s}{\tau_t N_t}$

Probability of each possible event (see Table S2)

Randomly select an event based on its probability of occurrence (see Table S2) Update the changes in the state of the cell (see $\Delta State$ in Table S2)

Increment time by $\frac{1}{\rho^t + \epsilon^t}$

Update the number of free ribosomes, R^{f}

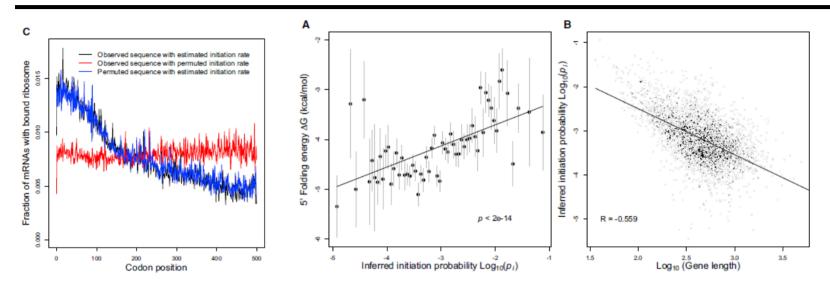
Update the number of free tRNAs of type $\phi(j)$, $T^{f}_{\phi(j)}$

end

1	Gene	mRNA #			laitiatian aata	Event week ability	104-4-
Initiation	#	of gene			Initiation rate	Event probability	⊿State
	1	1			0	0	N/A
	1	2			0	0	N/A
	1	3			$\frac{R^f p_1}{\tau_r N_r}$	$\frac{R^f p_1}{\tau_r N_r (\rho^t + \epsilon^t)}$	$R^f \rightarrow R^f - 1$
	1	A_1			$\frac{\frac{R^f p_1}{\tau_r N_r}}{$	$\frac{R^f p_1}{\tau_r N_r (\rho^t + \epsilon^t)}$	$R^f \to R^f - 1$
	2	1			$\frac{R^f p_2}{\tau_r N_r}$	$\frac{R^f p_2}{\tau_r N_r (\rho^t + \epsilon^t)}$	$R^f \to R^f - 1$
	2	2			$\frac{R^f p_2}{\tau_r N_r}$	$\frac{R^f p_2}{\tau_r N_r (\rho^t + \epsilon^t)}$	$R^f \rightarrow R^f - 1$
	2						
	2	A_2			0	0	N/A
	n						
	n	A_n			$\frac{R^f p_n}{\tau_r N_r}$	$\frac{R^f p_n}{\tau_r N_r (\rho^t + \epsilon^t)}$	$R^f \rightarrow R^f - 1$
				Total initiation rate	$\rho^t = \sum_{i=1}^n \frac{R^f f_i A_i p_i}{\tau_r N_r}$		
Elongation	Gene #	mRNA # of gene	Codon position	Ribosome bound	Elongation rate	Event probability	⊿State
	1	1	1	N	0	0	N/A
	1	1	2	Y	$\frac{T^f_{\phi(1,2)} w_{1,2} s}{\tau_t N_t}$	$\frac{T^f_{\phi(1,2)} w_{1,2} s}{\tau_t N_t (\rho^t + \epsilon^t)}$	Ribosome bound at codon $2 \rightarrow N$ Ribosome bound at codon $3 \rightarrow Y$
	1	1	3	Ν	0	0	N/A
	1	1					
	1	1	L_1	Ν	0	0	N/A
	1	2	1	Y	0	0	N/A
	1	2					
	1	2	11	Y	$\frac{T^{f}_{\phi(1,11)}w_{1,11}s}{\tau_{t}N_{t}}$	$\frac{T^f_{\phi(1,11)} w_{1,11} s}{\tau_t N_t (\rho^t + \epsilon^t)}$	Ribosome bound at codon $11 \rightarrow N$ Ribosome bound at codon $12 \rightarrow Y$
	1	2					
	1	2	L_1	Y	$\frac{T^f_{\phi(1,L_1)}w_{1,L_1}s}{\tau_t N_t}$	$\frac{T^f_{\phi(1,L_1)} w_{1,L_1} s}{\tau_t N_t (\rho^t + \epsilon^t)}$	$R^f \rightarrow R^f + 1$
	1						
	1	A_1	L_1				
	2						
	2	A_2	L_2				
	n	A_n	L_n				
				Total elongation rate	$\epsilon^{t} = \sum_{j=1}^{61} \frac{R^{b}(j)T^{f}_{\phi(j)}w_{j}s}{\tau_{t}N_{t}}$		

Table S2. Markov States and Transition Rates, Related to Figure 1

Is protein production initiation or elongation limited in exponential growing yeast populations?



more ribosomes at 5énd BUT due to >> intiation prob. on short genes

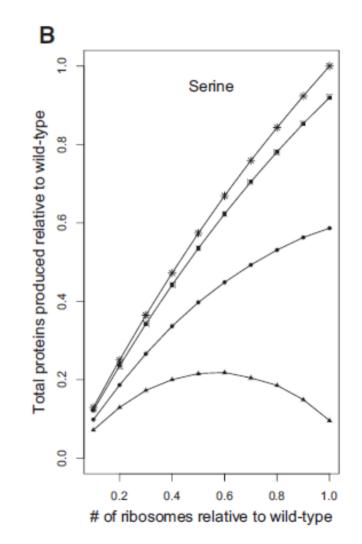
initiation limited

debugging of wrong inference from exp. data

Under amino-acid starvation down regulating ribosomes can increase protein production

because translation becomes elongation limited reducing Ribosomes increases free TRNA'

- + Wild-type amino-acid abundance
- 2-fold amino-acid starvation
- 5-fold amino-acid starvation
- 10-fold amino-acid starvation



conclusions event based modeling of stochastic reaction kinetics

Data intensive modeling

Quantitative conclusions

Upscaling to "whole cell modeling"

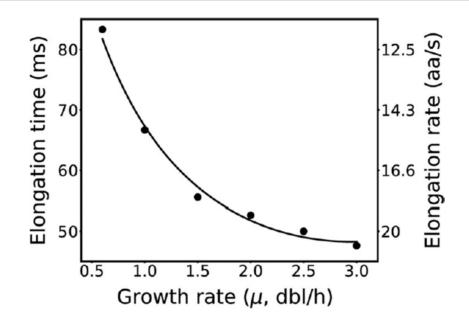
But note simplifications:

space but no spatial structure

fixed number of molecules

fixed conditions

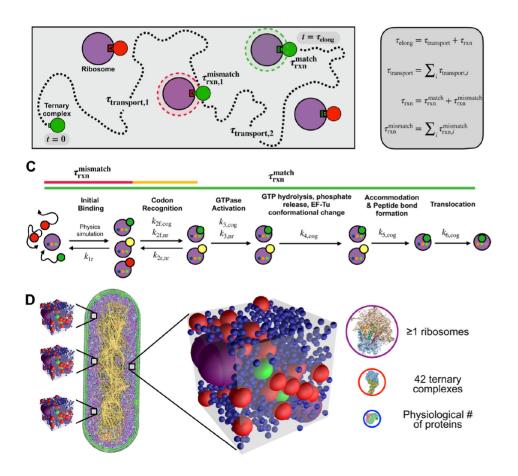
Further scruteny of traslation dynamics Higher efficiency at higher growth rates How??



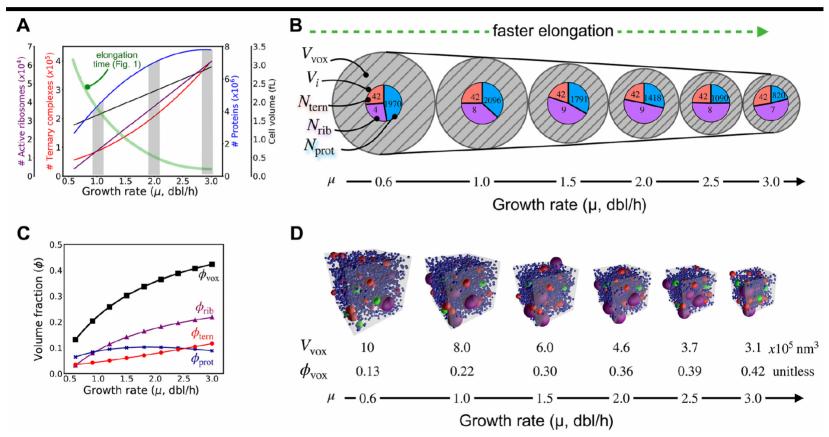
AJ Maheshwari, AM Sunol, E Gonzalez, D Endy 2023:

Colloidal physics modeling reveals how per-ribosome productivity increases with growth rate in escherichia coli

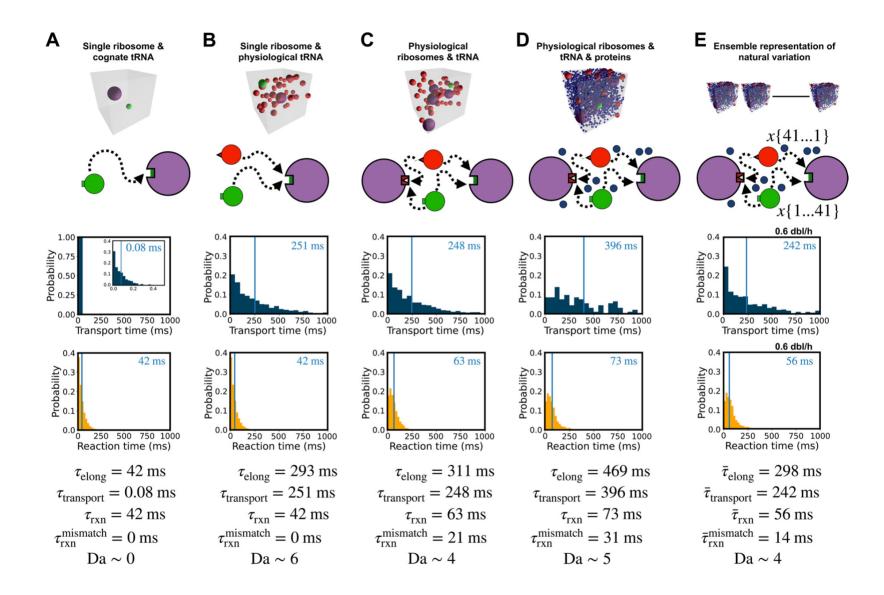
Detailed dynamics of elongation in ribosomes Analyse dynamics per "voxel"



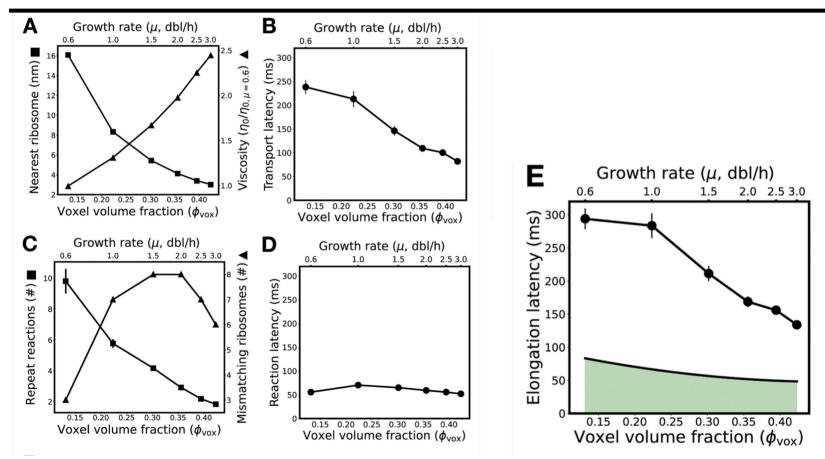
Molecular composition of E.coli cell dependent on growthrate



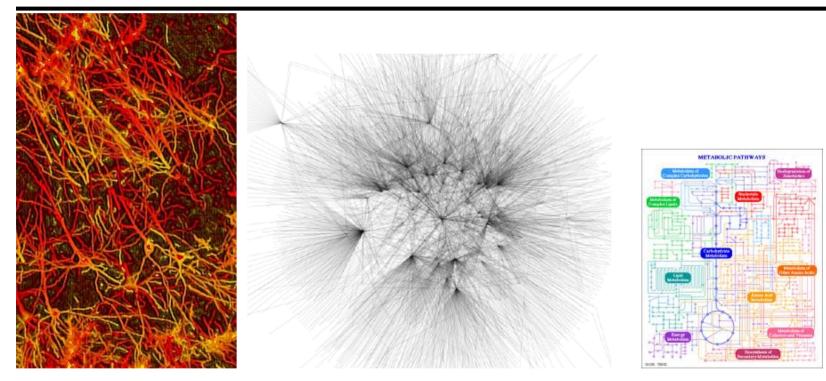
Charateristic times dependent on voxel composition: transport time dominate in "realistic compositions



Model explains speedup at higher growthrates shorter distances, but slower diffusion by crowding But not elongation rate, (parameter uncentainty??)



dynamical systems: decomposition in many simple systems cont., NETWORKS

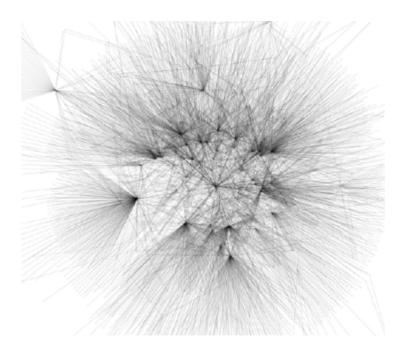


Neural net connected

yeast transcription net information transfer

Keg metabolic net mass conservation stochiometric

Gene regulation Networks: "full" transcription network of yeast



How does it behave?

how special is it?

(evolution)

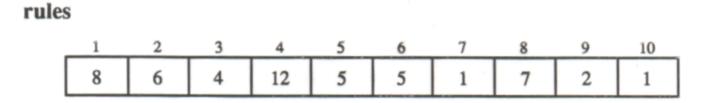
Boolean Networks

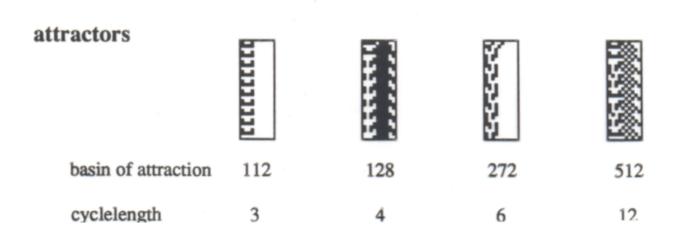
Proposed by S.Kauffmann (1969) as model for gene regulation

Like binary CA but specific network structure (IO relations) each node own transition rule (Boolean function with k inputs) studied: NK networks

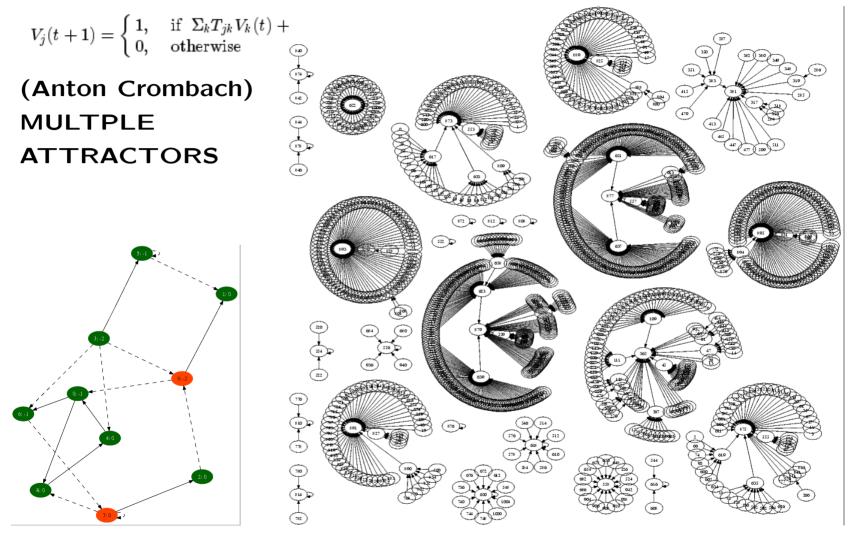
Boolean network : special cases can be mapped into CA (homogeneous network structure, "rule-layer")

Multiple attractors





simple random network (threshold dynamics)



ONLY 10 nodes (=genes)!

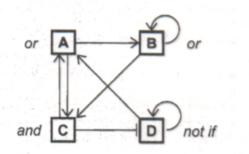
STATESPACE

What kind of behavior do we expect from gene regulation networks?

multiple attractors (cell types) alternative trajectories from A' and A'' to B multiple causes robustness (knockouts)

Huang S, Ingber D. Exp Cell Res. 2000

a Network wiring diagram



Boolean functions:

UTPUT
~
0 1 1

B: "	or "	
INP A	PUTS B	OUTPUT B
0	0	0
0	1	1
1	0	1
1	1	0

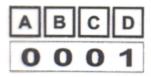
C: " and "

INP A	UTS B	OUTPUT C
0	0	0
0	1	0
1	0	0
1	1	1

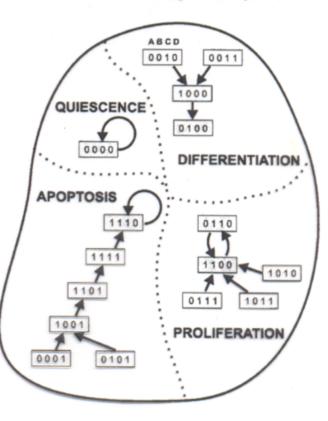


INP	UTS	OUTOUT
C	D	D
0	0	0
0	1	1
1	0	0
1	1	0

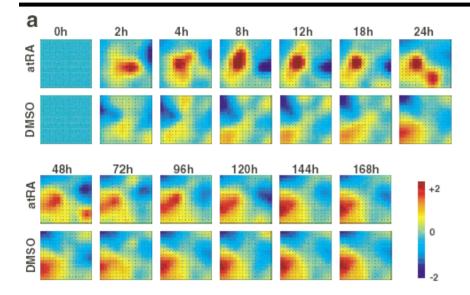
b A network state

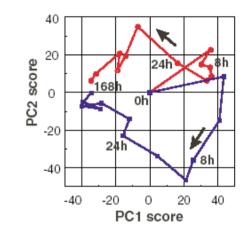


C Protein activity state space



2 pathways to Neutrophyl differentiation Huang et all 2005 (Phys Rev Letters)





gene expression through time

2773 dim state-space,

trajectories in 2D projection

 n^{2773} states!

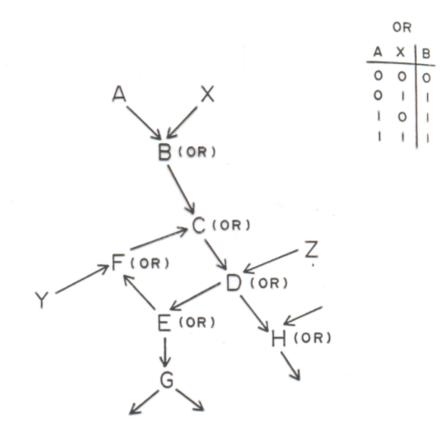
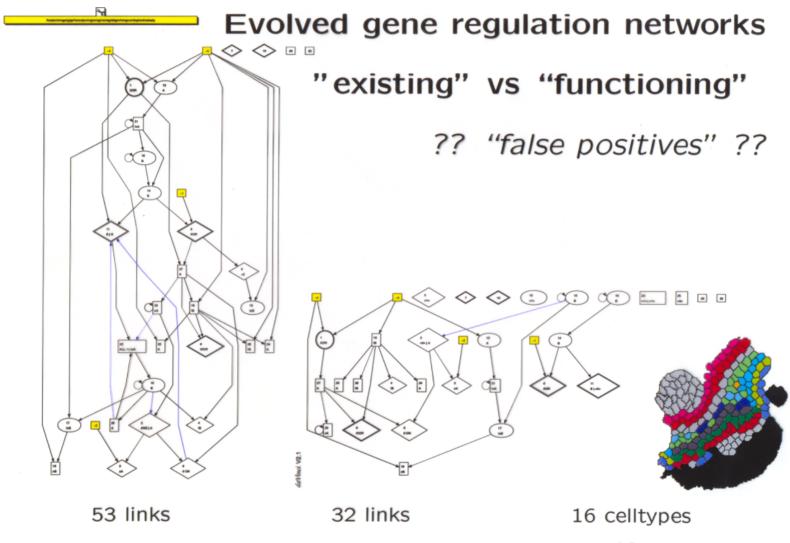


FIGURE 8 Forcing structure among binary elements governed by the Boolean OR function. The forcing "1" value propagates down structure and around forcing loop which eventually is "frozen" into the forced state with "1" values at all elements around the loop. Loop then radiates fixed forced values downstream. From *Origins of Order*: *Self Organization in Evolution* by S. A. Kauffman. Copyright © 1990 by Oxford University Press, Inc. Reprinted by permission.



18 reg. genes

aPlaci V2.1

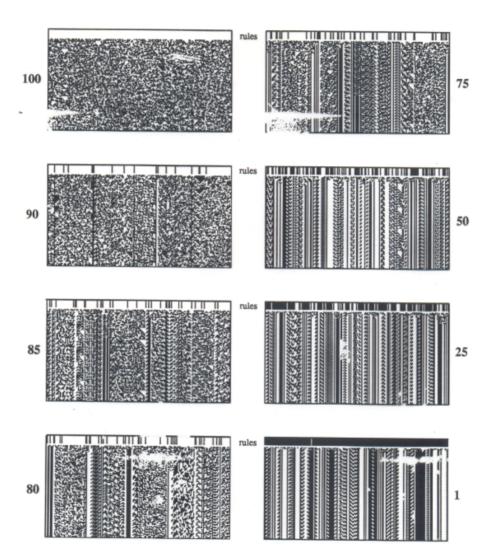
Properties of Random Boolean Networks (depending on K)

TABLE 1	Properties of Random Boolean Nets for Different Values of K^1				
	State Cycle Length	Number of State Cycle Attractors	Homeostatic Stability	Reachability Among Cycles After Perturbation	
K = N	$0.5 \times 2^{N/2}$	N/e	Low	High	
K > 5	$\begin{array}{l} 0.5\times2^{BN}\\ (B>1) \end{array}$	$\sim N\left[\frac{\log\left(\frac{1}{1/2\pm\alpha}\right)}{2}\right];$ $\alpha = p_{(K)} - 1/2$	Low	High	
K = 1	Very Long	Very Many	Low	High	
K = 2	\sqrt{N}	\sqrt{N}	High	Low	

¹ Column 1: state cycle length is median number of states on a state cycle Column 2: number of state cycle attractors in behavior of one net. ($\alpha = P_K - 1/2$, where P_K is mean internal homogeneity of all Boolean functions on K inputs; see text.) Column 3: homeostatic stability refers to tendency to return to same state cycle after transient reversal of activity of any one element Column 4: reachability is number of other state cycles to which net flows from each state cycle after all possible minimal perturbations, due to reversing activity of one element.

Importance of sampling method: Dependence on K is dependence on fraction (non) forcing rules!

Non forcing rules in 1D CA (k=2)



Important:

Identification of cell state with attractor of gene regulation network

Multiple attractors in simple networks

alternative trajectories to attracotr

Domain of attraction: i.e. "robusteness"

forcing functions i.e. "robustness"

NOT IMPORTANT (WRONG!) connectivity of 2 "ideal"

Functional Overlap and Regulatory Links Shape Genetic Interactions between Signaling Pathways Sake van Wageningen, Patrick Kemmeren,..... Berend Snel and Frank C.P. Holstege Cell Dec 2010

141 kinases, 38 phosphatases in Yeast.

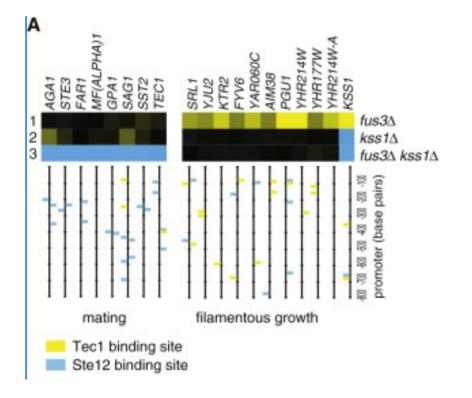
60% single knockouts "no phenotype" (= < 8 genes different of WT) (single growth condition)

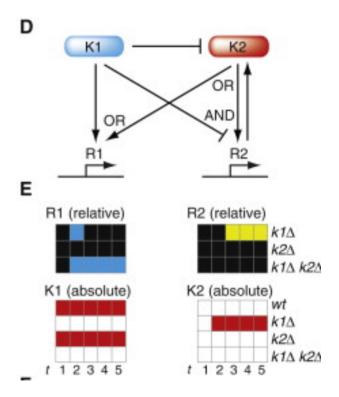
Double knockouts: 21 "buffering" s with other kinase/phosphatasse v

double knockout expression profiles

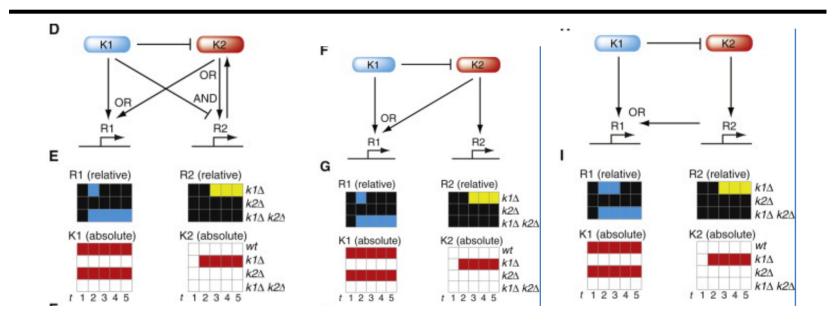
	ark1 Δ prk1 Δ ark1 Δ prk1 Δ
$\begin{array}{c c} ptp 2 \Delta & ptp 2 \Delta \\ ptp 3 \Delta & ptp 2 \Delta \\ ptp 2 \Delta ptp 3 \Delta & ptp 2 \Delta ptp 3 \Delta \\ \end{array}$	$yck1\Delta$ yck2 Δ inviable yck1 Δ yck2 Δ
В	
	$ptc2\Delta$ $ptc1\Delta$ $ptc1\Delta$ $ptc1\Delta$ $ptc2\Delta$
	$pph3\Delta$ $ptc1\Delta$ $ptc1\Delta$ $ptc1\Delta$ $pph3\Delta$
С	
$ \begin{array}{c} fus3\Delta \\ kss1\Delta \\ fus3\Delta kss1\Delta \\ fus3\Delta kss1\Delta \\ \end{array} $	hsl1∆ cla4∆ hsl1∆ cla4∆
bck1 Δ bck1 Δ bck1 Δ cla4 Δ to cla4 Δ bck1 Δ ptp3 Δ bck1 Δ cla4 Δ to cla4 Δ bck1 Δ cla4 Δ bck1 Δ ptp3 Δ bck1 Δ bck1 Δ ptp3 Δ bck1 Δ ptp3 Δ bck1 Δ bck1 Δ ptp3 Δ bck1 Δ	$mih 1\Delta$ $elm 1\Delta$ $mih 1\Delta elm 1\Delta^*$
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	slt2∆ ptp3∆ slt2∆ ptp3∆
D cka1\Delta cka2\Delta inviable cka1\Delta cka2\Delta inviable ptk1\Delta ptk2\Delta inviable sky1\Delta ptk2\Delta inviable hsl1\Delta mih1\Delta	ypk2 Δ ypk1 Δ inviable ypk1 Δ ypk2 Δ

example of mixed epistasis filamentous growth vs mating





2 simpler networks with same effect (complexer network most similar to exp. inferred network)



Many networks (max 2 inputs per node) with same effect!

Edges	Models	Correct models	Root models
2	0	0	0
3	352	0	0
4	4,960	2	2
5	32,896	6	1
6	129,280	24	8
7	294,912	28	7
8	331,776	46	10

all buffering pairs: Many non-homologs!; many mixed

Table 1. Buffering Relationships between Kinases and Phosphatases							
Gene 1	Gene 2	Туре	Duplication	Time (Years Ago)	Buffering Relationship		
HAL5	SAT4	kk	old	600 M – 2 G	complete redundancy		
ARK1	PRK1	kk	whole genome	125 M	complete redundancy		
PTP2	PTP3	PP	recent	125 M - 600 M	complete redundancy		
YCK1	YCK2	kk	whole genome	125 M	complete redundancy ^a		
PTC1	PTC2	PP	old	600 M – 2 G	quantitative redundancy		
PTC1	PPH3	PP	not homologous		quantitative redundancy		
PBS2	PTK2	kk	ancient	>2G	mixed epistasis		
CLA4	SLT2	kk	ancient	>2G	mixed epistasis		
CLA4	H\$L1	kk	ancient	>2G	mixed epistasis		
SNF1	RIM11	kk	ancient	>2G	mixed epistasis		
BCK1	PTP3	kp	not homologous		mixed epistasis		
SLT2	PTP3	kp	not homologous		mixed epistasis		
FUS3 ^b	KSS1	kk	recent	125 M - 600 M	mixed epistasis		
ELM1	MIH1	kp	not homologous		mixed epistasis ^o		
CLA4	BCK1	kk	ancient	>2G	mixed epistasis ^o		
DUN1	PPH3	kp	not homologous		mixed epistasis ^o		
CKA2	CKA1	kk	recent	125 M - 600 M	not classified ^a		
YPK1 ^b	YPK2	kk	whole genome	125 M	not classified ^a		
PTK1	PTK2	kk	whole genome	125 M	not classified ^a		
HSL1	MIH1	kp	not homologous		not classified ^a		
SKY1	PTK2	kk	ancient	>2G	not classified ^a		

regulatory network via mixed response networks

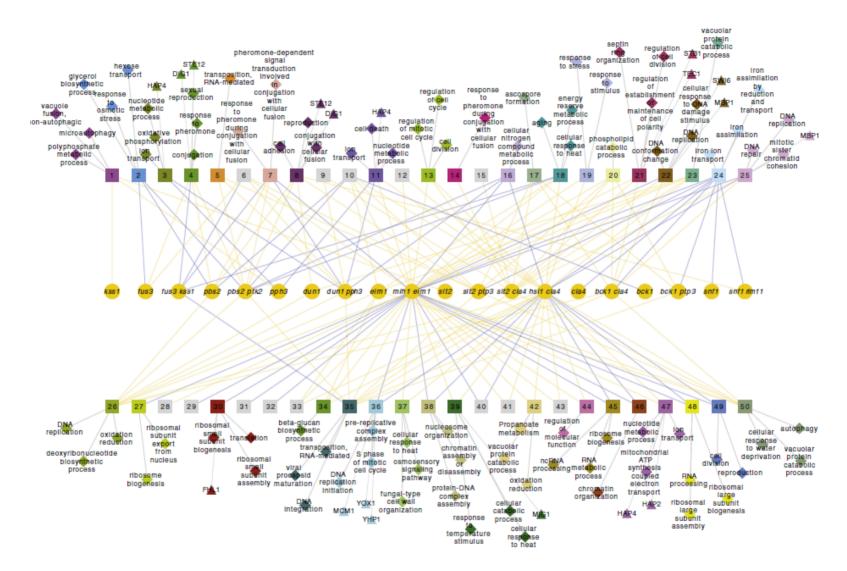


Figure 6. Multiprocess Control through Signaling Components with Mixed Epistasis

Inference of (Boolean) GRN from timeseries dynamic and static "accuracy"

VERY Active research:Google Scholar 2023: *"gene regulatory network inference"*4930 hits: Baysian, deep NN, random forestsheuristics: conform to known structural features

E.G. performance assessed from simulated boolean networks (extracted from E.coli GRN database) . Pušnik, M.Mraz, N.Zimicand M.Moškon 2022

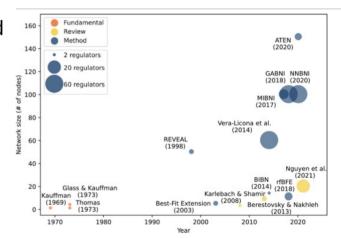
Fairly good Dynamic accuracy

Poor static accuracy (many different measures) TP, FP, TN, FN in different combi's

hard because:

stochasticity, missing data, very large search space AND

"redundant regulation": minimal or "true" network? multiple regulators with different Boolean functions produce the same results



some measurements of prediction quality

$$Precision = \frac{TP}{TP+FP}.$$
(8)

On the other hand, recall presents a fraction of correctly inferred edges among all edges in the initial network:

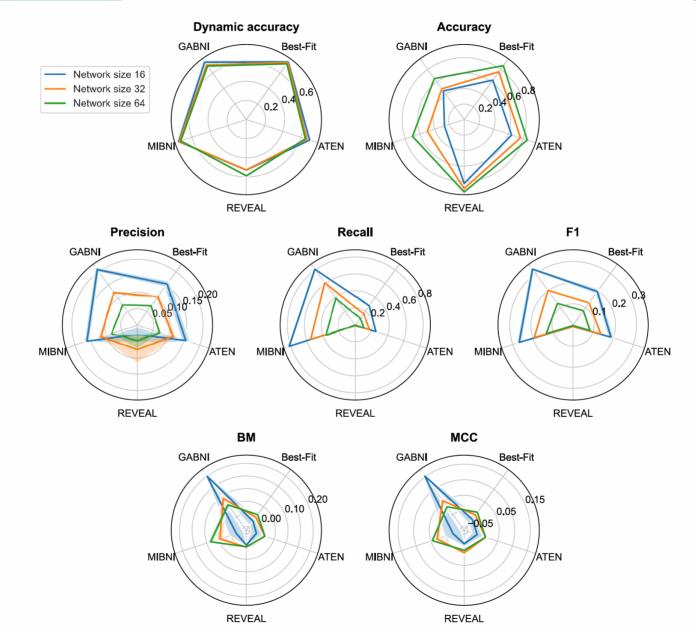
$$Recall = TPR = \frac{TP}{TP + FN}.$$
(9)

Precision and recall are important metrics, since we are more interested in edges than in non-edges. Accuracy is the proportion of all correct predictions, including edges and non-edges:

$$Accuracy = \frac{TP + TN}{TP + TN + FP + FN}.$$
(10)

F1 score is defined as a <u>harmonic mean</u> of the precision and recall:

$$F1 = 2 \cdot \frac{Precision \cdot Recall}{Precision + Recall}.$$
(11)



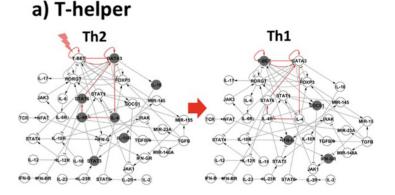
Finding attractor (stable cell states) positive feedback loops

Finding "hubs"

HOW TO SWITCH CELL STAT == how to switch attractors

Examples of minimal set of perturbations needed to switch cell states calculated from Boolean network models and verified in experiments.

Despite simplifications usefull predictions



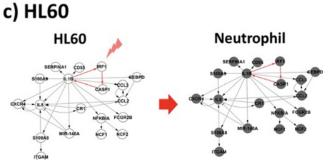
b) EMT

Mesenchymal



Epithelial





Crespo et al. BMC Systems Biology 2013

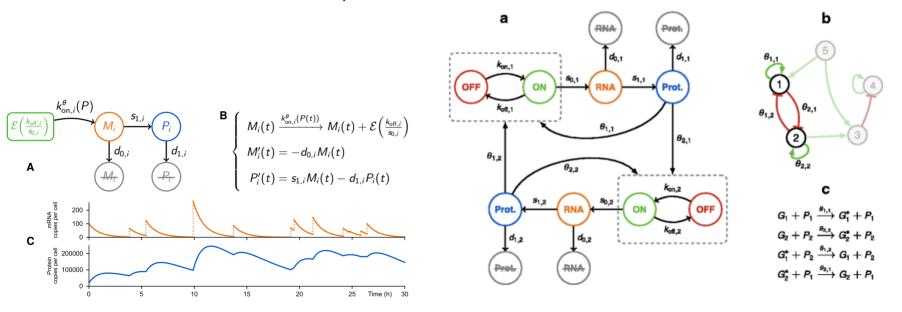
- not on/off but quantitative response. e.g. modeled as set of ODE's with sigmoid response sizes
- mRNA --> protein
- Stochastic binding/unbinding of TF on DNA binding sites; gene expression in bursts
- Competition for binding sites overlap of binding sites for different TF and competition for TF

•

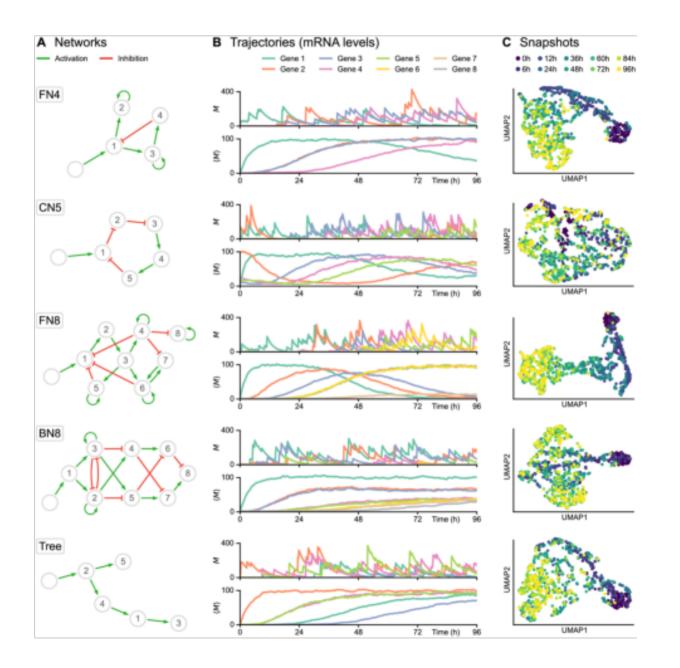
insights are obtained by multiple (wrong) models (Caricatures)

Stochastic gene expression single cell gene expression signatures

gene expression often in bursts, folowed by slow defradation of mRNA and buildup/decrease of protein



Elias Ventre, Olivier Gandrillon 2023, PLOS Comp Bio.



Coding structure of gene regulatory networks e.g. global epigenetic factors and competition for binding sites

Α **Epigenetic Factors** Local GRN Gene 1 Competition for binding sites F_1 ---of the Genome PRE/TRE TE Binding Sit Gene 2 Global epigenetic factors F_2 PRE/TRE TF Binding Sit bind at very many places Rest but they are in limited numbers -----PRE/TRE TF Binding Sit Model by distinguishing General model bound/unbound states С В of (overlapping) binding sites, Activating TF Activator Kand EF and TF Unbound Neutral Active Repressed

PRE/TRE state

Repressor P

TF binding site state

Other

Genes

Bound

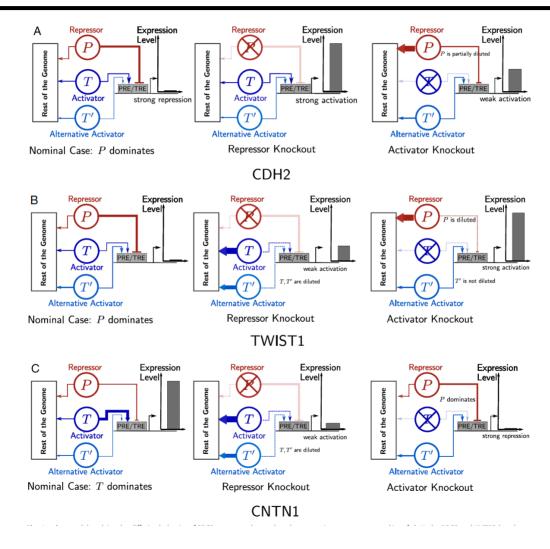
Can lead to very counter intuitive outcomes.

Examples from the The Polycomb (repressors) and Trithorax Groups (activators) of EFs which modulate histon tails. Very many targets (e.g. PRC3 10% of genes in embryonic stem cells)

Epigenetic factor competition reshapes the EMT landscape

M. Ali Al-Radhawi... Herbert Levine PNAS 2022

some modeled and experimentally observed examples everything possible by tuning the parameters...



Event based models (2) Individual based models (IBM,IOM,agent based models)

simple rules -> complex behavior

Simplest form:

Individual simple (in)finite state machine "schedules" its own next "event" in continuous time Interacts with (potentially complex) environment and other individuals like it

LOCAL information determines behavior

Variable structure: not invariant set of interaction partners (in contrast to CA, Boolean nets)

distributed (shared) environmental "memory" --> flexible behaviour from rigid rules / automatic adaptation

The best model of the world is the world internal model of the world as "crux" for information shortage

contexts Ethology; Ecology, Evolution, (also transcription) swarm intelligence 'intelligence without reasoning (Brooks)'

simple rules to complex behavior

cf " Simon (1969)

"an ant seen as a behavioral system is quite simple the apparent complexity of its behavior is due to the complexity of the environment in which it finds itself"

" a human seen as a behavioral system is quite simple the apparent complexity of his behavior is due to the complexity of the environment in which it finds himself "

4

TODO as alternative explanation for observed behavior Social structure as side-effect of foraging

> Question: social structure of chimpanzees Why all males groups in Chimpanzees? Why single females? Why do males travel further?

Modeling strategy: Make model WITHOUT behavior we are interested in

(but include some basic structure of system under consideration) and OBSERVE

individuals: (CHIMPS)

 go to nearest fruit tree and eat until satisfied or fruit exhausted - rest
 males : search for receptive females - females eat protein food not eaten by males

environment: GOMBE-like

----> Social structure of Chimpanzees

opportunity vs optimality based explanation

Hogeweg & Hesper 1990; te Boekhorst H. 1994

MCHIMP

- iſ DARK then SLEEP
- elseif there is a CIIIMP at 15(DIST(100 (ANGLE (120)then if TUMESCENT FCIIIMP then FOLLOW else GO TO the CIIIMP most in front and if there is FRUIT at DIST <10 then EAT else REST (.RAND .02 .03)
- elseif there is a FRUIT at 5 < DIST < 100 then GO TO FRUIT most in front and EAT
- else FORWARD (RAND 25 40) if just eaten then REST (.3 * amount eaten) else REST (RAND .02 .03)

FRUIT

1200 (variable --> ca 250) (600 1800) number 1 - 35 chimphours size renewel 5 - 10 days

(2-70, 1-23)

PROT

FCHIMP

- iſ DARK then SLEEP
- elseif there is a FRUIT at 5 < DIST < 100 then GO TO FRUIT most in front and EAT
- elseif there is a PROT at 5 < DIST < 100 ANGLE<120 then GOT TO FRUIT most in front and EAT
- else FORWARD (RAND 25 40) if just eaten then REST(.3 * amount eaten) else REST(RAND .02 .03)

number 250 fixed (125 275) .03 * FRUIT size renewel when eaten

MCHIMP

ìſ DARK then SLEEP

elseif there is a CHIMP at 15(DIST(100 (ANGLE (120)then if TUMESCENT FCIIIMP then FOLLOW else GO TO the CIIIMP most in front and if there is FRUIT at DIST <10 then EAT else REST (.RAND .02 .03)

- elseif there is a FRUIT at 5 < DIST < 100 then GO TO FRUIT most in front and EAT
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FRUIT

number size renewel

1200 (variable --> ca 250) (600 1800) 1 = 35 chimphours 5 - 10 days

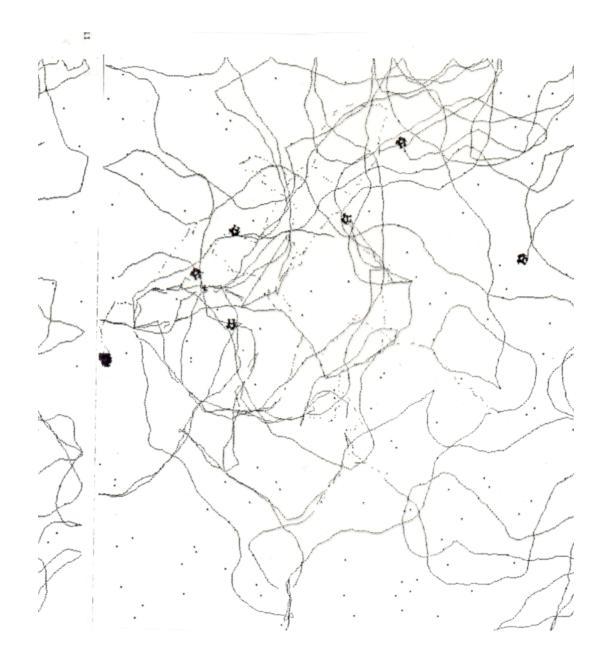
(2-70, 1-23)

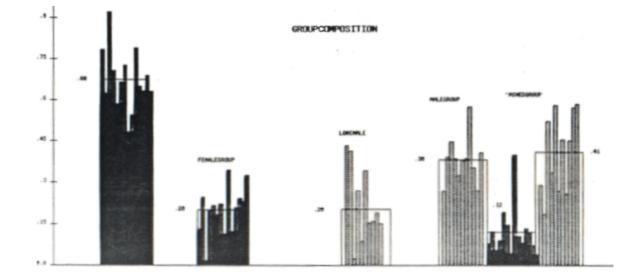
PROT

FCHIMP

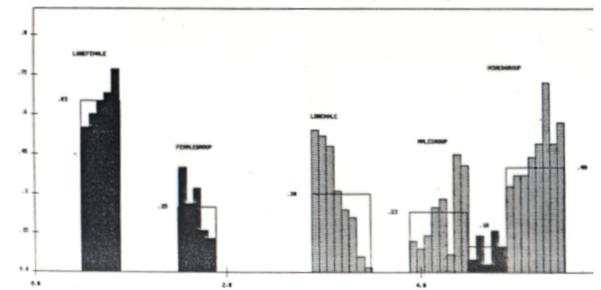
- iſ DARK then SLEEP
- there is a FRUIT at 5 < DIST < 100 then elseif GO TO FRUIT most in front and EAT
- elseif there is a PROT at 5 < DIST < 100 ANGLE<120 then GOT TO FRUIT most in front and EAT
- FORWARD (RAND 25 40) else if just eaten then REST(.3 * amount eaten) else REST(RAND .02 .03)

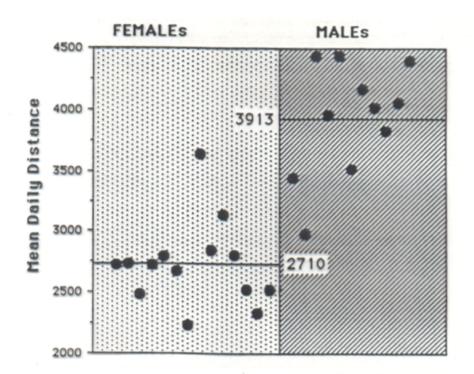
250 fixed (125 275) number size 03 * FRUIT renewel when eaten





GROUPCOMPOSITION IN GOMBE 1972-1973 (HAPLERIN 1979)





exp: Females 2.7 Km Males 4 Km

Fig. 5. Distance travelled by CHIMPs in the standard environment. Average values of individual CHIMPs are shown data from MALEs are in the dark shaded area.

Much studied prototypes:

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flocking birds (BOIDS, Reynolds)
schooling fish (e.g. Hemelrijk) migrating herds (locusts (Couzin), wilde-
beest (Levin))
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Mostly (continuous) force-based models: attraction, repulsion, aligning relative to neighboring 'beasts' (variable set)

Different behaviours by different ranges of vision (angle) repulsion/attraction/aligning

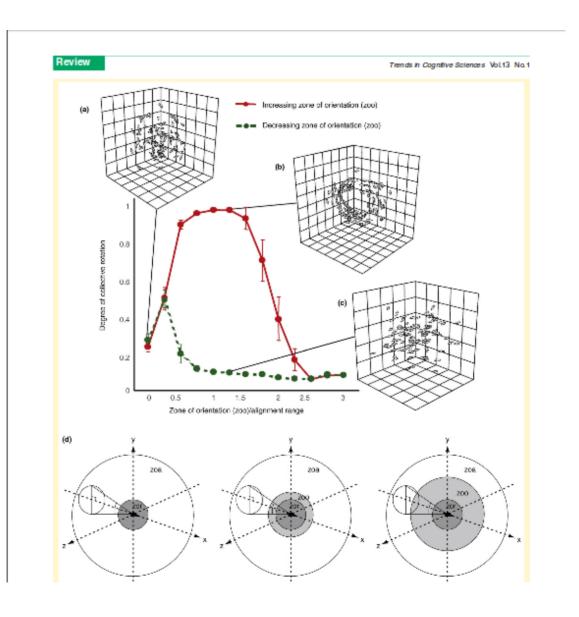
minimal models or more physics of environment (air/water/)

NO environmental memory

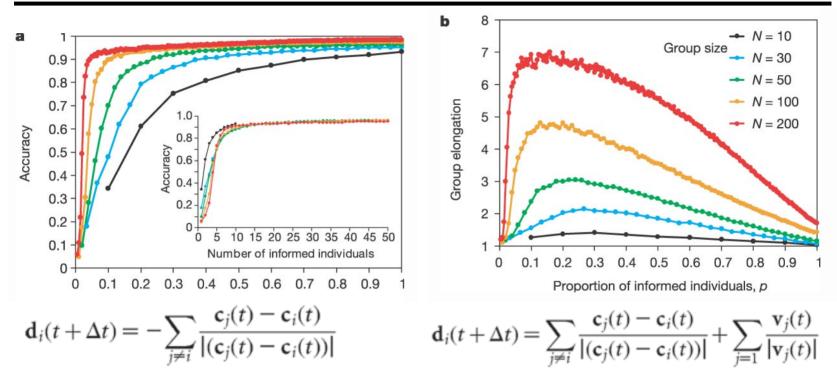


inert environment basic grouping modes; bistability

from Couzin 2009, Trend cogn science



Effective decision making in flocks and schools Couzin, Nature 2005



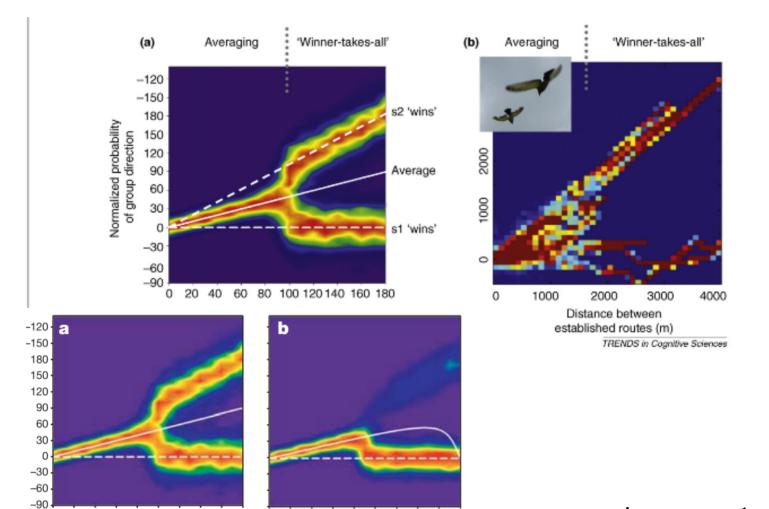
repulsion

attraction + alignment

$$\mathbf{d}_{i}'(t + \Delta t) = \frac{\hat{\mathbf{d}}_{i}(t + \Delta t) + \omega \mathbf{g}_{i}}{|\hat{\mathbf{d}}_{i}(t + \Delta t) + \omega \mathbf{g}_{i}|}$$

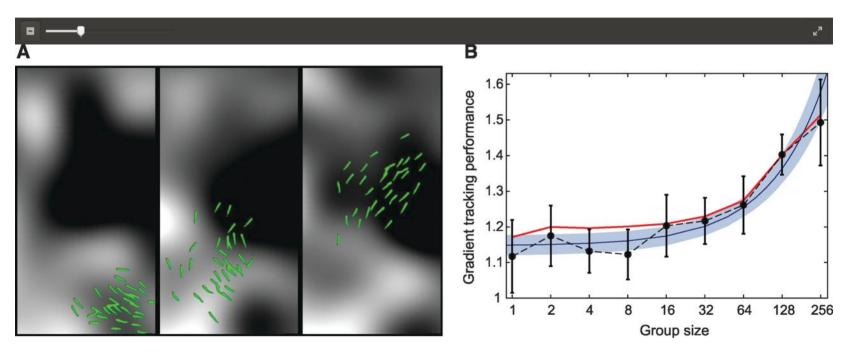
purpose:

conflict resolution in schools and flocks



0 20 40 60 80 100 120 140 160 180 0 20 40 60 80 100 120 140 160 180 ONE MORE in group1

photo-taxis in fish groups, Berdahl,..,Couzin, Science 2013



Fish move slower in the dark

Larger schools can find dark places better