
interlocking ecological and evolutionary timescales

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Interlocking timescale: Eco-evolutionary model (van der Laan and Hogeweg)

A simple discrete Lotka-Volterra type model has been used with equations:

$$\frac{\Delta X_i}{\Delta t} = aX_i - bX_i \sum_{j=1}^n X_j - cX_i \sum_{j=1}^n \alpha_{ij} Y_j + \mu \{0.5(X_{i-1} + X_{i+1}) - X_i\}$$

$$\frac{\Delta Y_i}{\Delta t} = -dY_i + ecY_i \sum_{j=1}^n \alpha_{ji} X_j + \mu \{0.5(Y_{i-1} + Y_{i+1}) - Y_i\}$$

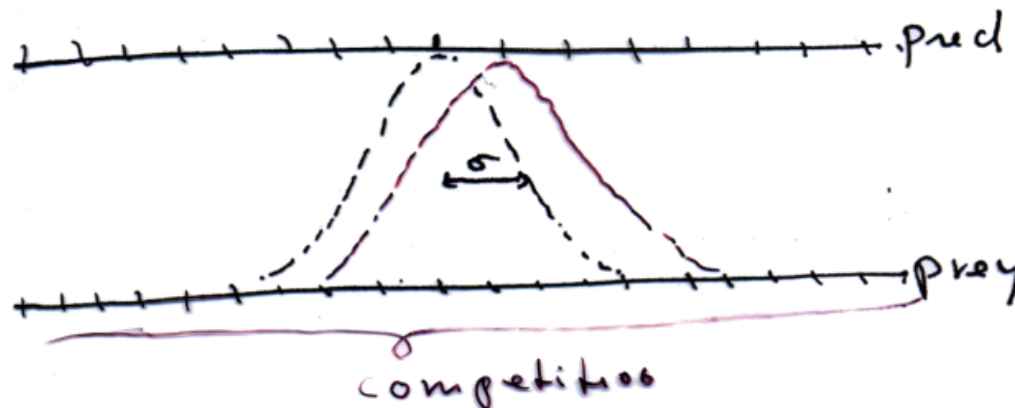
The Gaussian function for the interaction parameter is

$$\alpha_{ij} = \frac{1}{\sigma} e^{-(\text{Dist}(i,j)_{\min})^2 / 2\sigma^2}$$

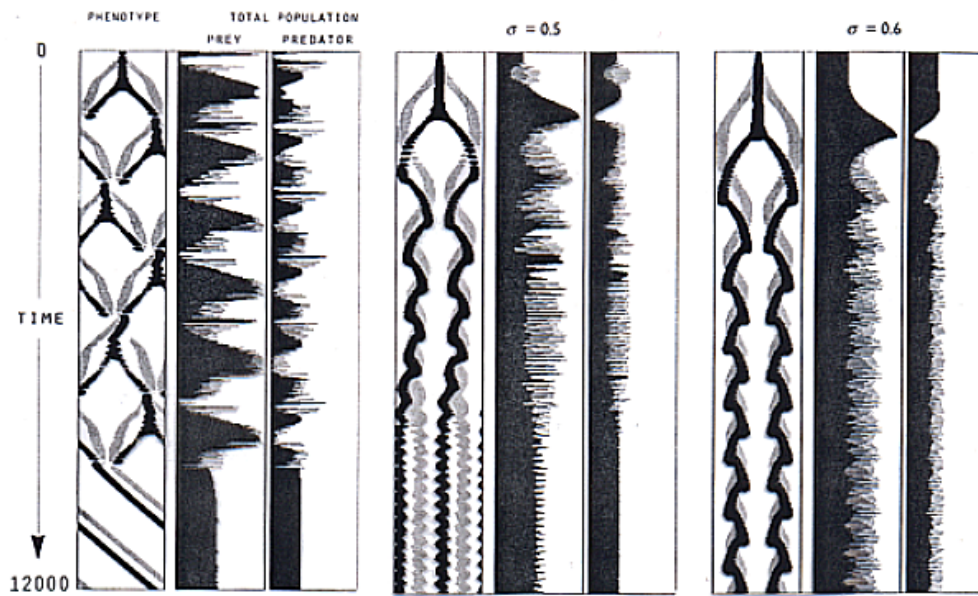
and α ranges from $\frac{1}{\sigma}$ to $\frac{1}{\sigma} e^{-1/2\sigma^2}$.

TABLE 1. Parameters of the eco-evolutionary model

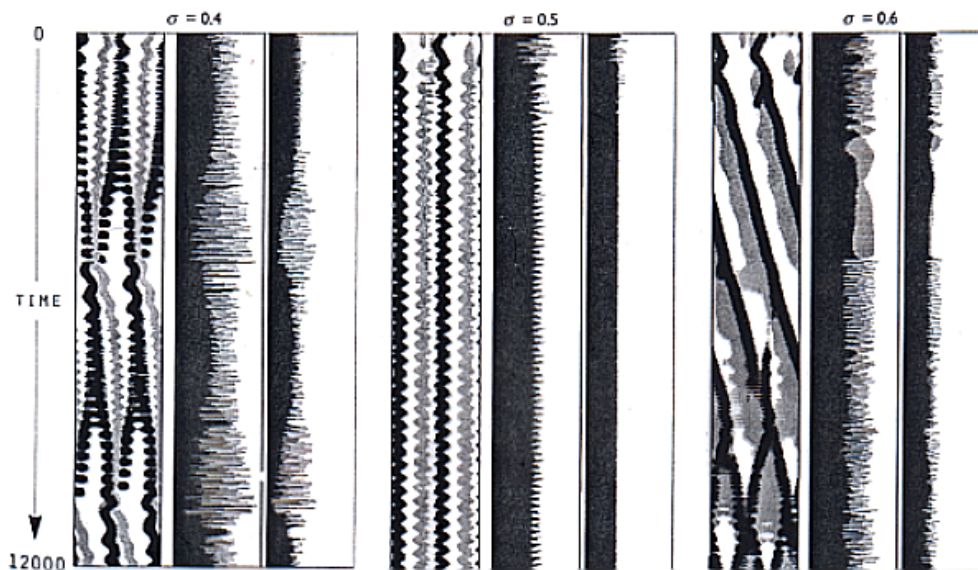
a	1.0	natural rate of increase for prey
b	0.005	prey competition parameter
c	0.0055	interaction parameter (fixed part)
α	variable	interaction parameter (evolvable part)
d	0.5	mortality of predator
e	0.73	efficiency of predator
θ	0.00001	threshold density
n	60	total number of phenotypes (length of axis)
μ	0.001	mutation rate
σ	0.4 to 0.6	standard deviation of Gaussian interaction curve



$\sigma = 0.4$ SYMMETRIC INITIAL CONFIGURATION



RANDOM INITIAL CONFIGURATION



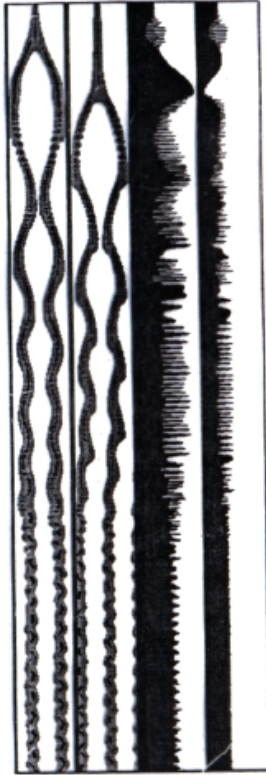
phenotype ppsize
prey predator prey predator



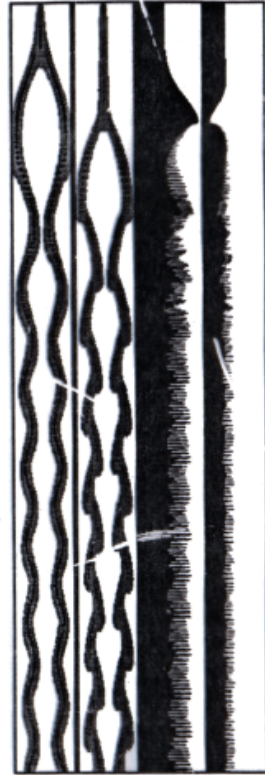
$\sigma = 0.4$
(a)

initiation : 1 prey + 1 pred.
→ (repeated) speciation

time
↓



$\sigma = 0.5$
(b)

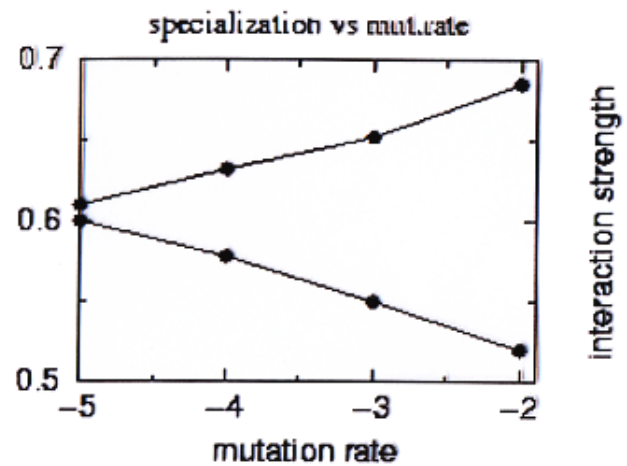
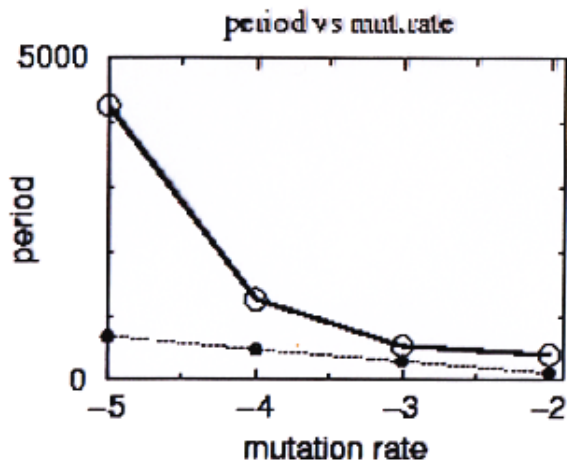
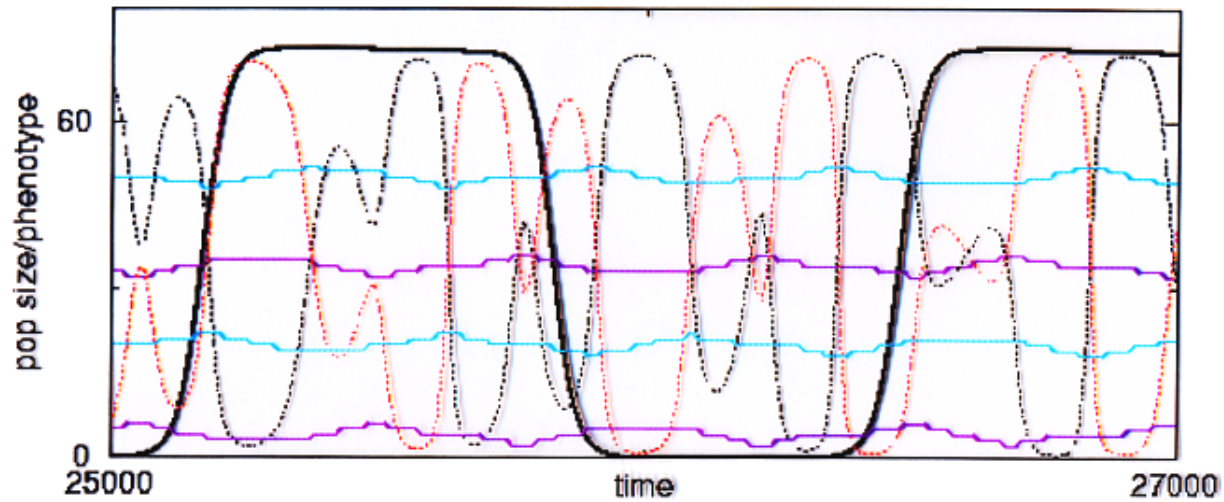


$\sigma = 0.6$
(c)

**Fallacy of separation of timescales:
ecological timescale > eco-evolutionary timescale**

eco- vs eco-evol dynamics

repl.rate = 1; mut.rate = .0001



conclusion: ecological vs eco-evolutionary dynamics

Evolutionary (mutational) variation can stabilize ecosystem

stopping mutation \rightarrow collapse of ecosystem

Nevertheless different lineages ('species')
with different niches (ecological functions)

Species and interactions selected for how they cope with mutation rates.

speciation(?)

compare this example, quasispecies, question 5b ₄